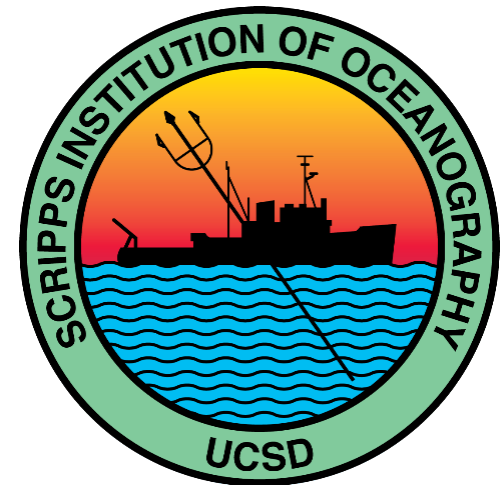


Optics of Marine Particles

Lecture 1

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IOCCG Summer Lecture Series

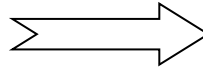
22 July - 2 August 2014, Villefranche-sur-Mer, France

What is ocean optics?

In principle it sounds straightforward, but in reality it's not...

Seawater is a highly complex medium containing a “witch's brew” of dissolved substances and suspended particles which strongly alter its optical properties.

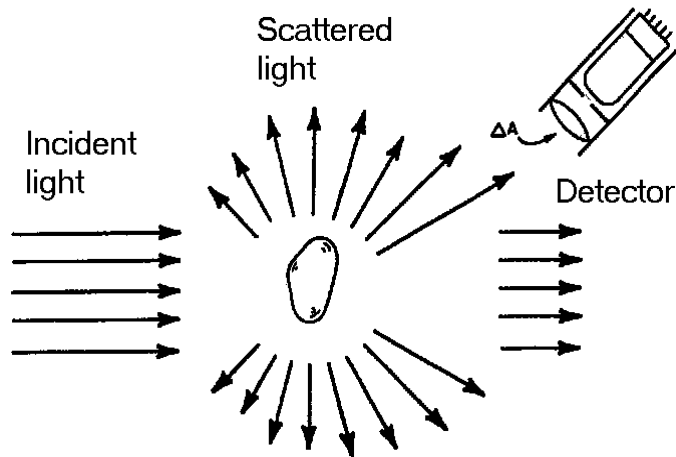
Microscopic plankton



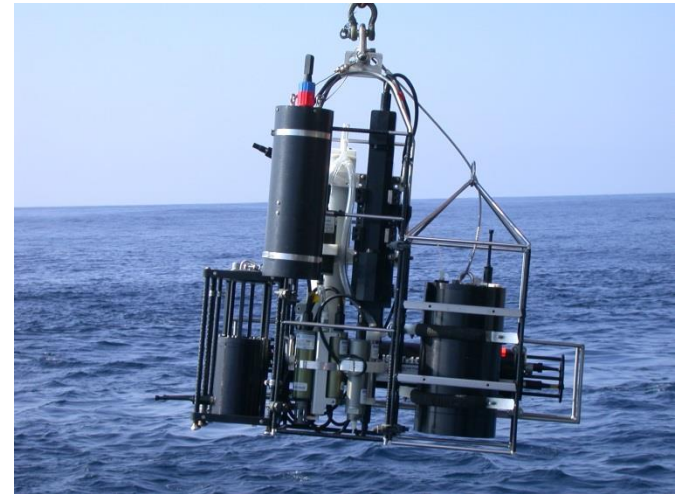
Because of this, ocean optics is a strongly interdisciplinary science combining physics, biology, chemistry, geology, and atmospheric sciences.

OCEAN OPTICS RESEARCH LAB AT SIO

PARTICLE OPTICS



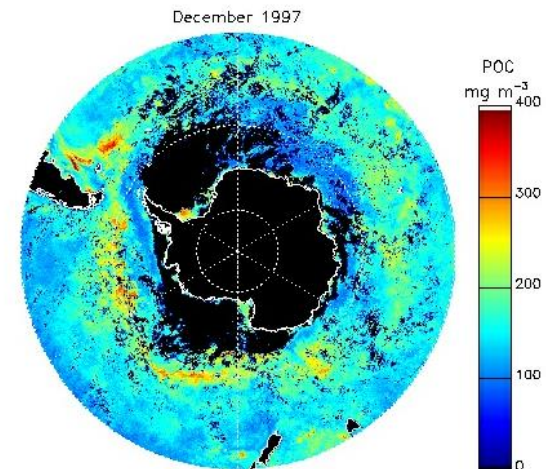
FIELD OBSERVATIONS



MODELING

$$\begin{aligned} \cos \theta \frac{dL(z, \xi, \lambda)}{dz} = & -c(z, \lambda)L(z, \xi, \lambda) \\ & + \int_{\Xi} L(z, \xi', \lambda) \beta(z, \xi' \rightarrow \xi, \lambda) d\Omega(\xi') \\ & + S(z, \xi, \lambda) \end{aligned}$$

REMOTE SENSING

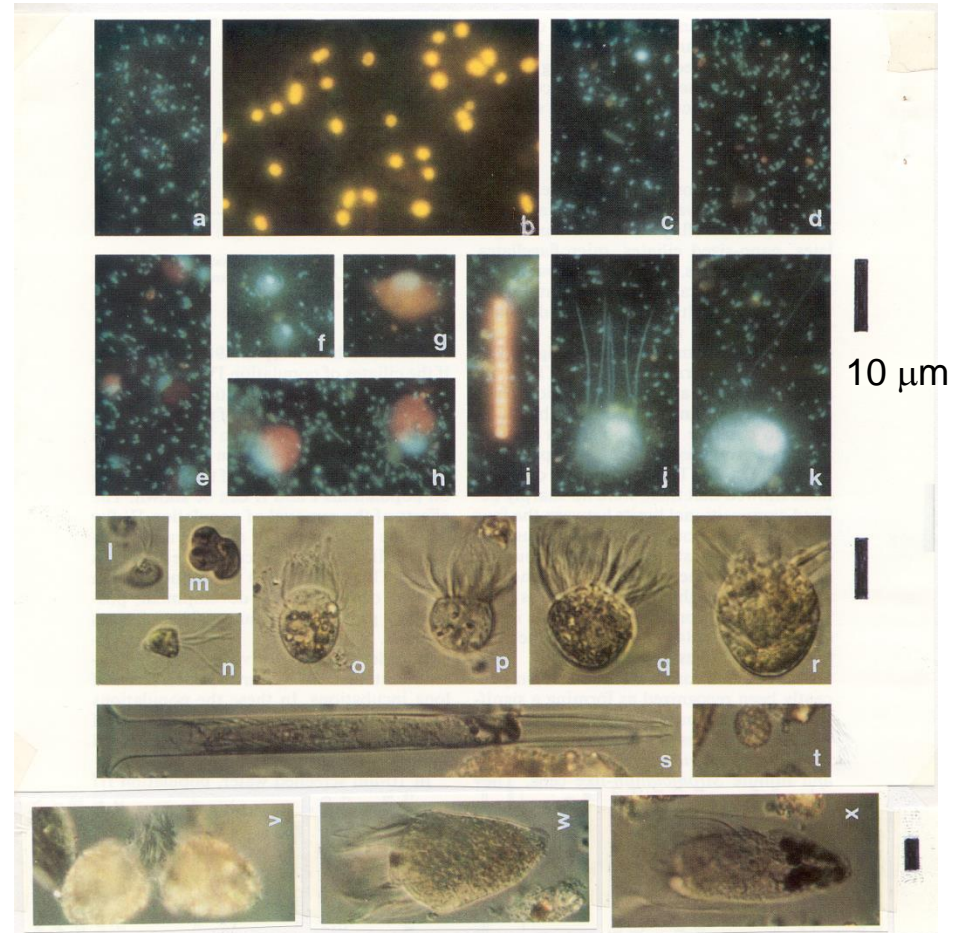
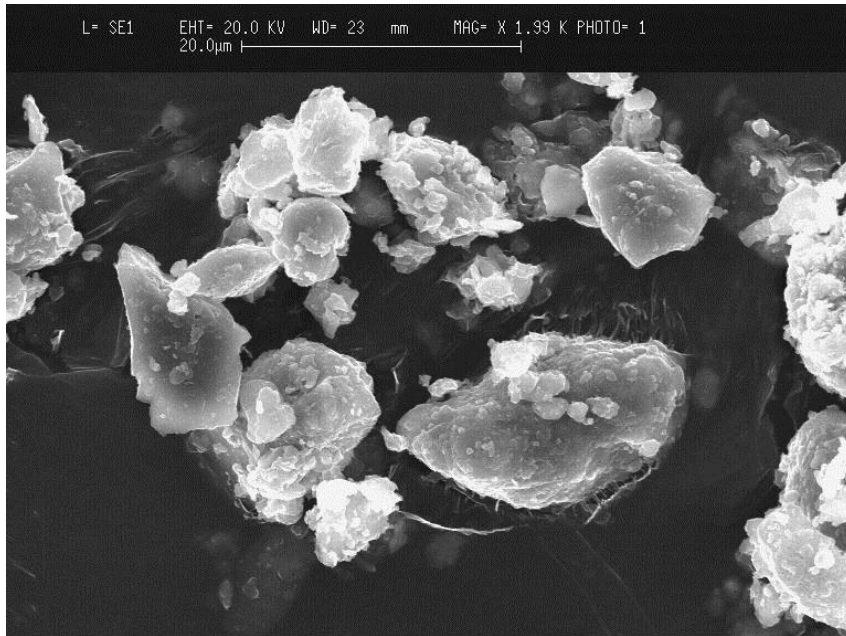


Seawater is a complex optical medium with a great variety of particle types and soluble species

- Molecular water
- Inorganic salts
- Dissolved organic matter
- Plankton microorganisms
- Organic detrital particles
- Mineral particles
- Colloidal particles
- Air bubbles

Suspended
Particulate
Matter

Diversity of biological and mineral particles

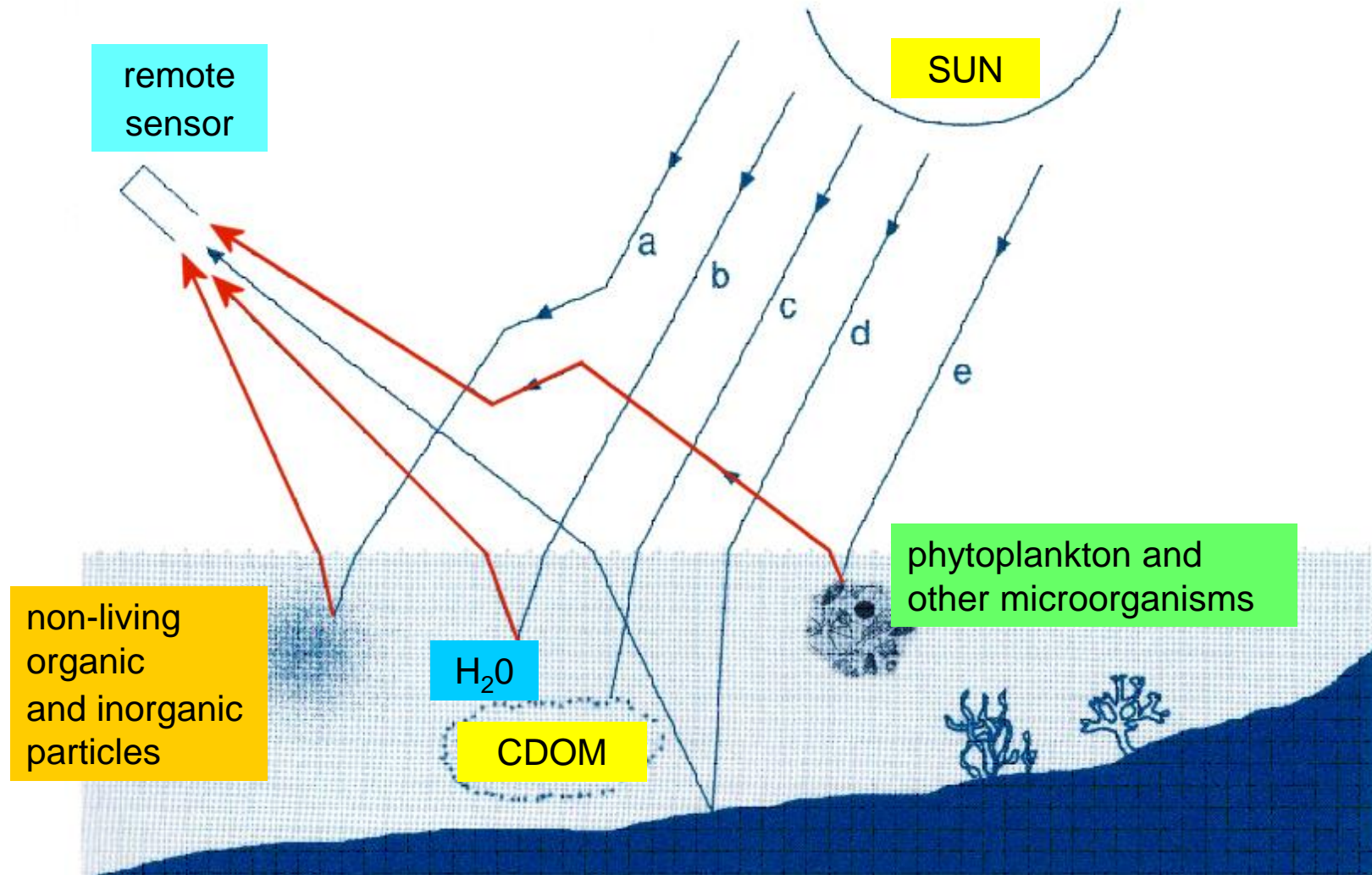


Long-term goals

- Understand the magnitudes and variability of oceanic optical properties
- Predict ocean optical properties given the types and concentration of suspended particles (*forward problem*)
- Obtain bio-optical properties and biogeochemical information from optical in situ and remote-sensing measurements (*inverse problem*)

OCEAN COLOR

$$R_{rs}(\lambda) \equiv \frac{L_w(\lambda)_{z=0^+}}{E_d(\lambda)_{z=0^+}} \propto \frac{b_b(\lambda)}{a(\lambda)}$$



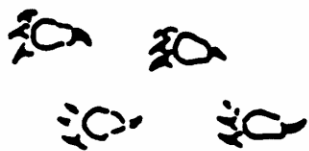
Direct problem



?

Tracks

Inverse problem

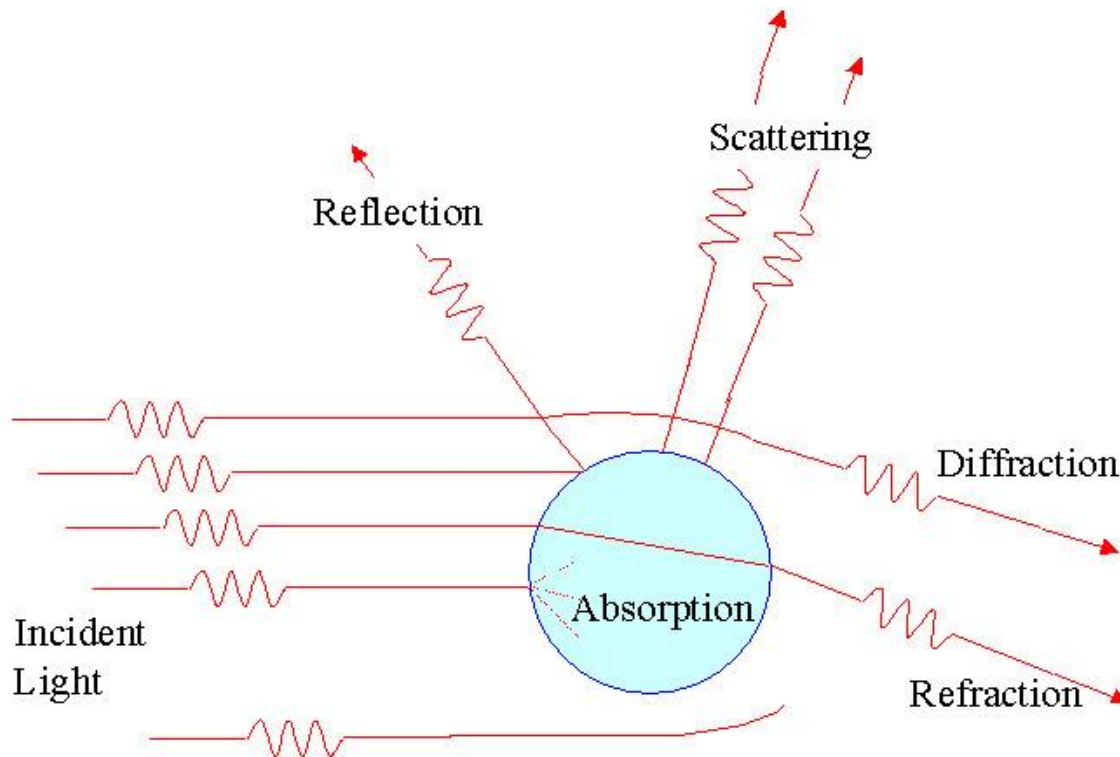


?

Dragon

Interaction of light with matter

Scattering - life of a photon



Absorption - death of a photon

**“Physics should be made
as simple as possible,
but no simpler”**

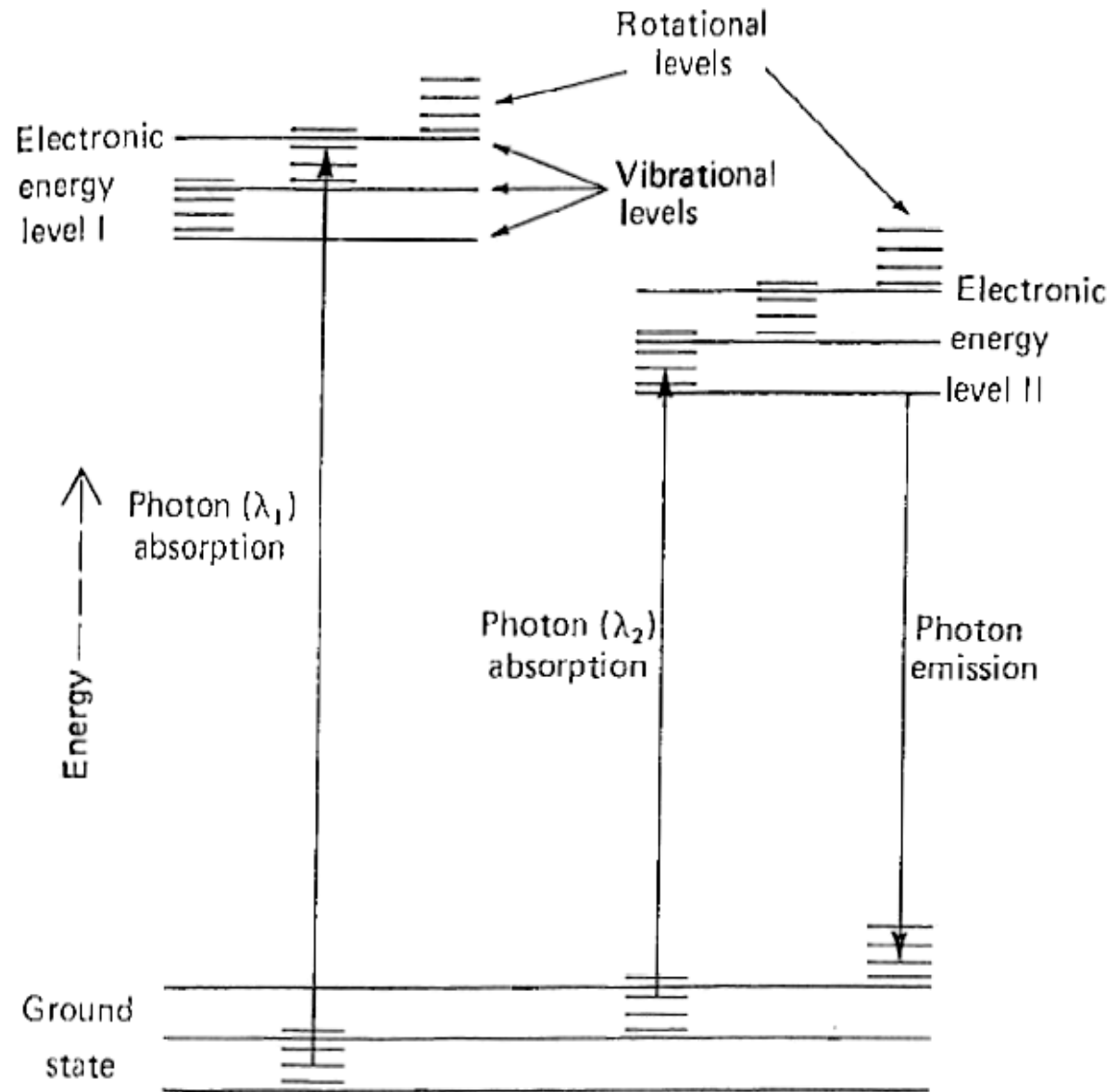
- Albert Einstein

Energy levels of molecules: Mechanism of light absorption

Electronic:
energy ~ 400 kJ/mol
 $\lambda \sim 100 - 1000$ nm

Vibrational:
energy $\sim 4 - 40$ kJ/mol
 $\lambda \sim 1 - 20$ μm

Rotational:
energy $\sim 10^{-2} - 10^{-3}$ kJ/mol
 $\lambda > 20$ μm



Absorption efficiency factor for particles

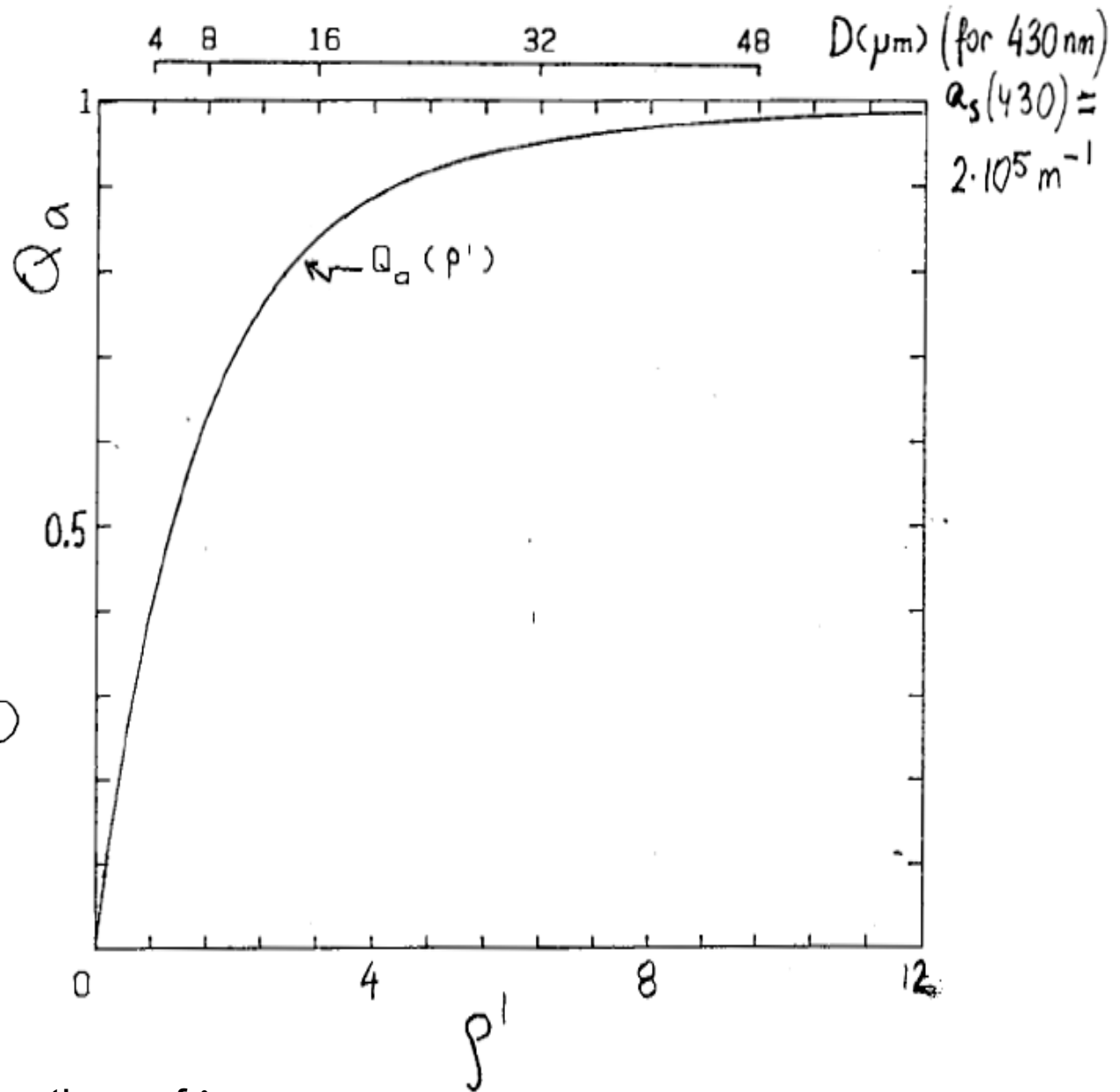
$$Q_a(\lambda) = F_a(\lambda) / F_o(\lambda)$$

particle in water

$$\rho' = 4 \alpha n' = a_s D$$

$$\alpha = \frac{\pi \cdot D \cdot n_w}{\lambda}$$

$$n' = \frac{\lambda a_s}{4 \pi n_w}$$



Note: Q_a , a_s , and n' are functions of λ

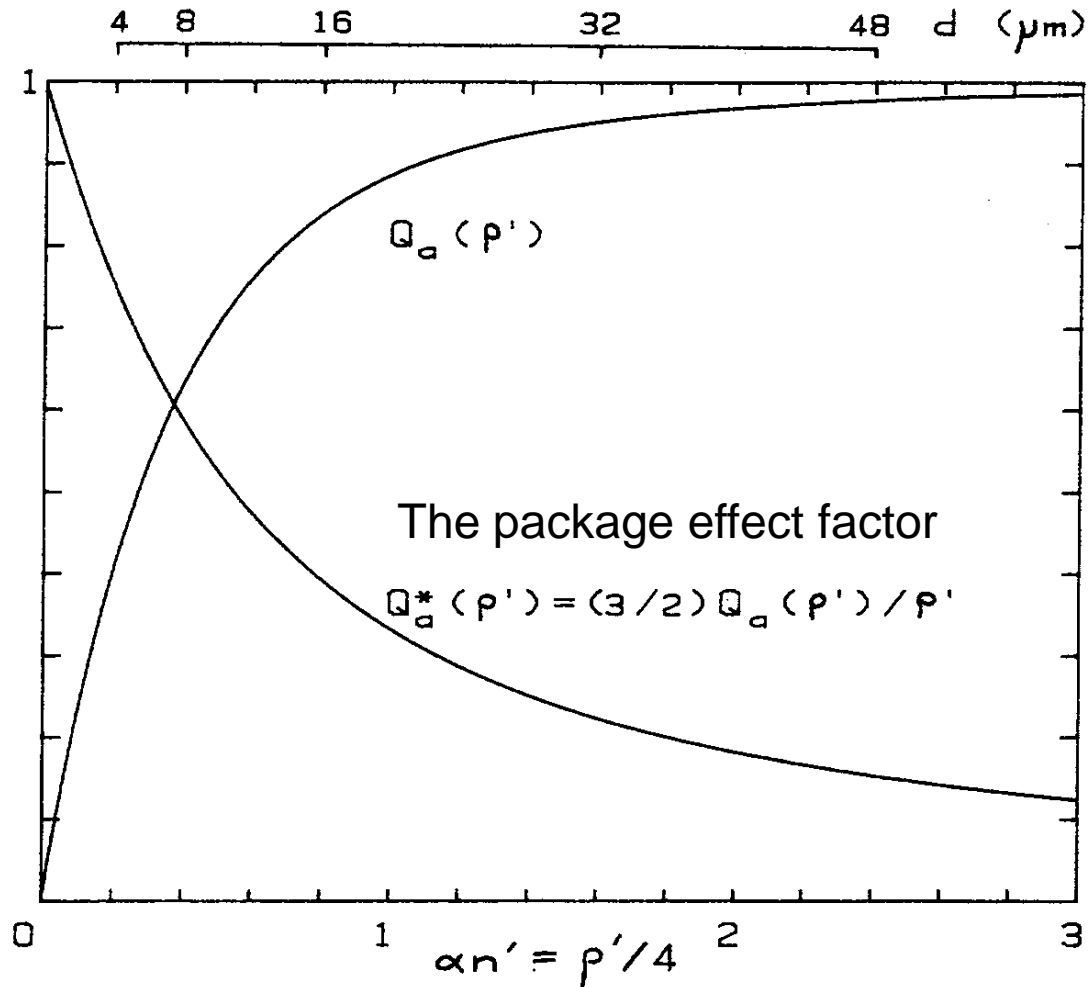


Fig. 1. Dimensionless functions Q_a and Q_a^* (equations 1 and 6) plotted vs $\alpha n'$. The corresponding scale in diameter d (μm) is obtained assuming that the absorption coefficient, a_{cm} , for the cellular material is equal to $2 \times 10^5 \text{ m}^{-1}$, which is a representative mean value for many algal cells at $\lambda = 430 \text{ nm}$ (see text). Note that $\rho' = da_{cm} = 4\alpha n'$.

Linkage between the single-particle optical properties and bulk optical properties of particle suspension

$$a = (N/V) Q_a G = (N/V) \sigma_a$$

a is the absorption coefficient of a collection of particles in aqueous suspension (units of m^{-1})

N/V is the number of particles per unit volume of water (units of m^{-3})

Q_a is the absorption efficiency factor (dimensionless)

G is the area of cross section of a particle (units of m^2).
For spherical particles $G = (\pi/4)D^2$ where D is a diameter

$\sigma_a (= Q_a G)$ is the absorption cross-section (units of m^2)

Note: a , Q_a , and σ_a are the spectral quantities (i.e., functions of light wavelength)

The package effect

$$a^* = a / Chl = a / [(Chl_{\text{cell}} / V_{\text{cell}}) (N/V) V_{\text{cell}}] = a / [Chl_i (N/V) V_{\text{cell}}]$$

For spherical particles:

$$a = (N/V) Q_a (\pi/4) D^2 \quad \text{and} \quad V_{\text{cell}} = (\pi/6) D^3$$

$$\begin{aligned} a^* &= (3/2) Q_a / (Chl_i D) = (3/2) (a_s / Chl_i) [Q_a / (a_s D)] = \\ &= (3/2) (a_s / Chl_i) (Q_a / \rho') = (a_s / Chl_i) Q_a^* = a_{\text{sol}}^* Q_a^* \end{aligned}$$

where $a_{\text{sol}}^* = a_s / Chl_i$

$$a^* = a_{\text{sol}}^* \quad \text{if} \quad \rho' \rightarrow 0 \quad \text{and} \quad Q_a^* = 1$$

The package effect factor:

$$Q_a^* = a^* / a_{\text{sol}}^* = (3/2) Q_a / \rho' = (3/2) Q_a / (a_s D)$$

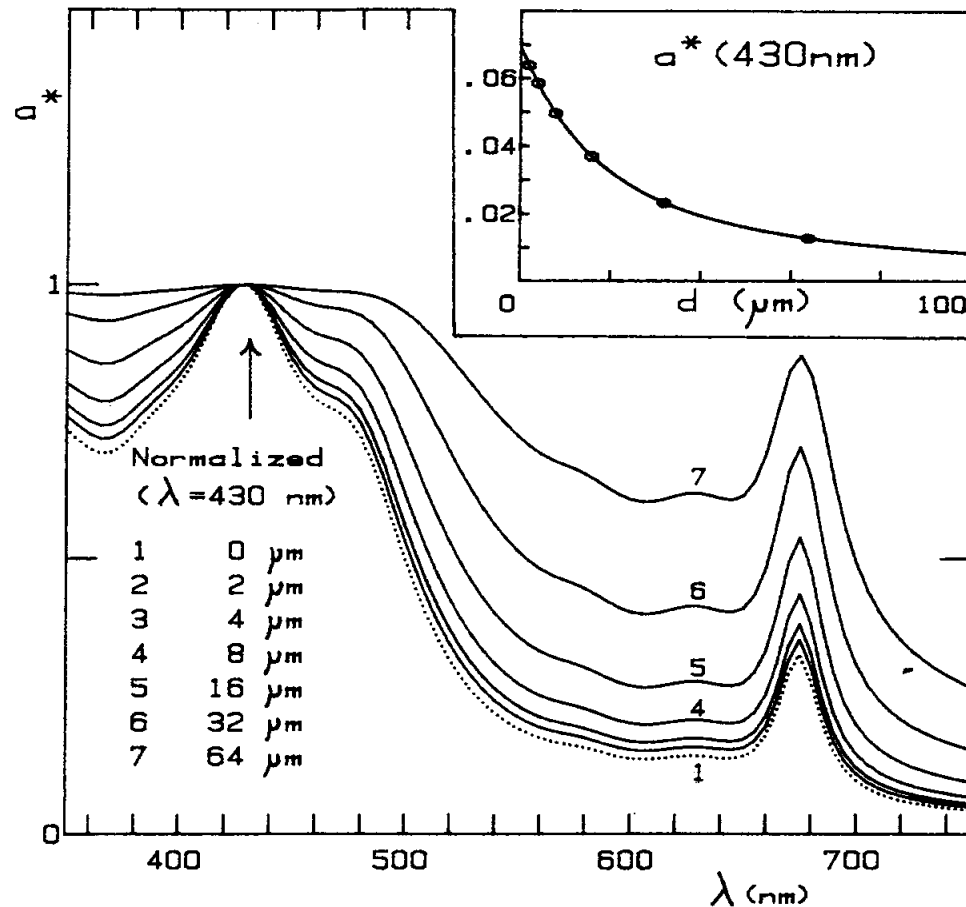
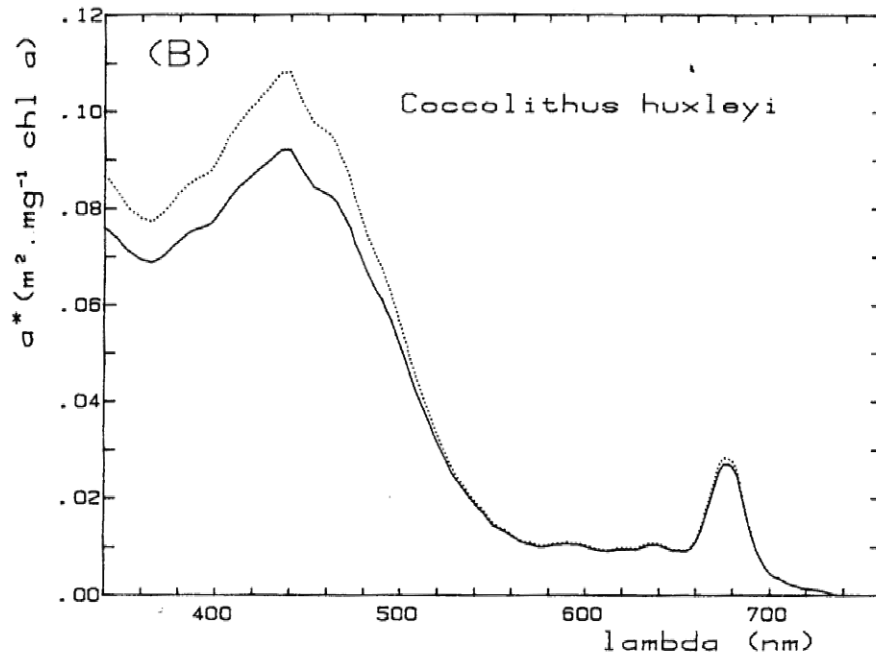
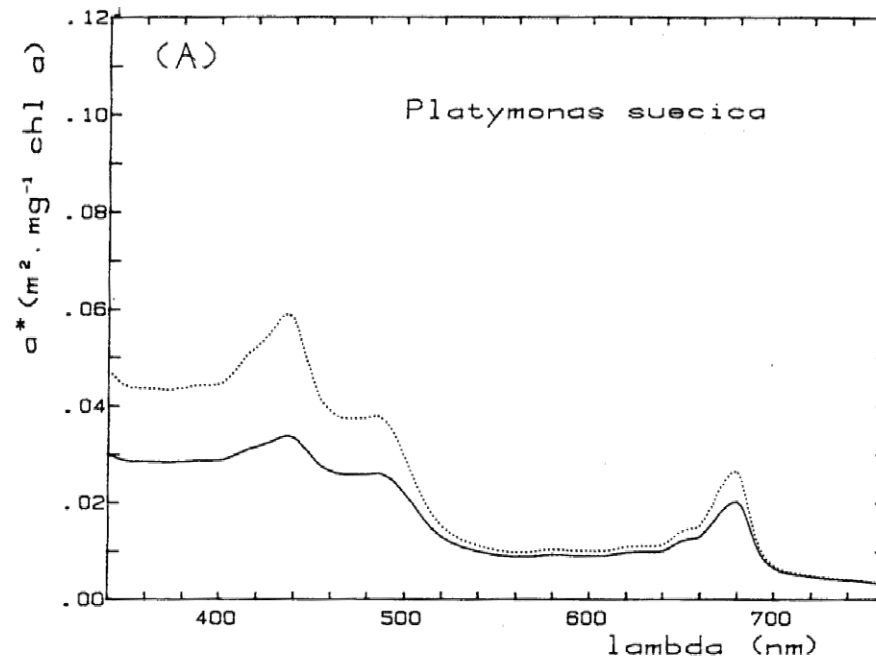


Fig. 2. Change in spectral absorption values with variable cell size (diameter, d , in μm) whereas the cell material forming the cells remains unchanged. The spectral absorption values of this material, somewhat arbitrarily adopted, are shown as the dotted curve. All curves are normalized, at $\lambda = 430$ nm, to evidence the progressive deformation. The variations with size of the specific absolute value at 430 nm ($\text{m}^2 \text{mg}^{-1}$ Chl a) are shown in inset, under the same assumption of a constant absorption of the cell material ($a_{cm} = 2 \times 10^5 \text{ m}^{-1}$ at 430 nm) and with the additional assumption of a constant intracellular pigment concentration ($c_i = 2.86 \times 10^6 \text{ mg Chl } a \text{ m}^{-3}$).

Solid lines: intact
cells in cultures

Dotted lines:
hypothetical
aqueous solution
of the material
forming the cells



(Morel and Bricaud 1981)

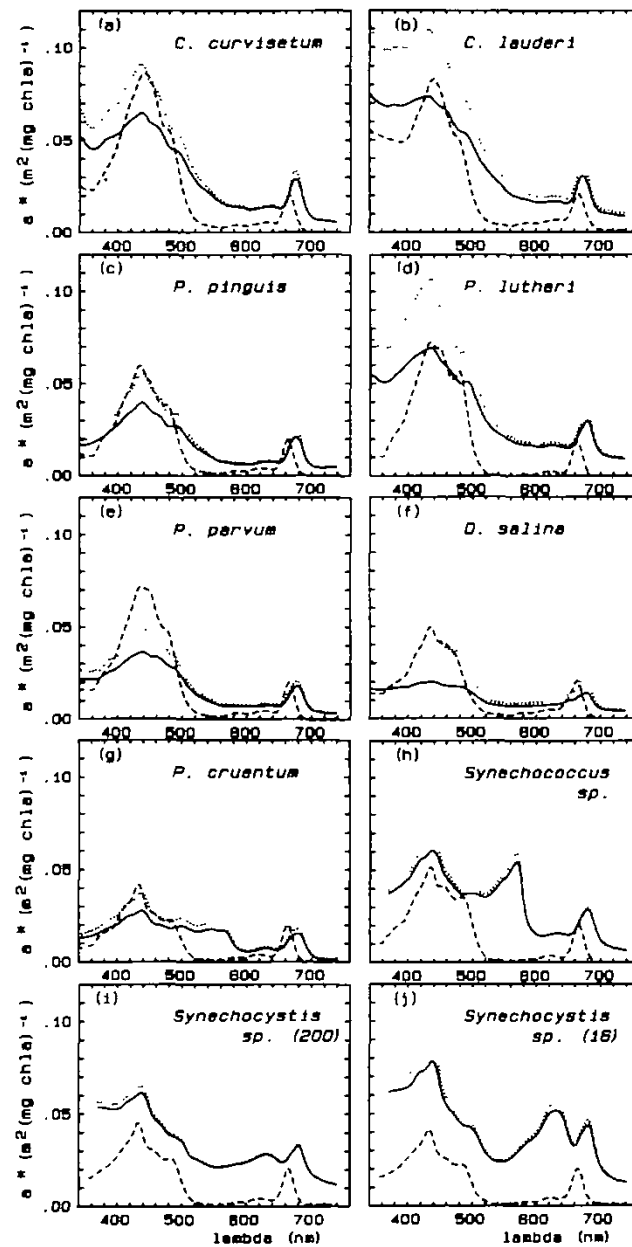


Fig. 1. Spectral values of the chl *a*-specific absorption coefficients measured for intact cells [$a^*_{\text{sus}}(\lambda)$, solid line], computed for a hypothetical aqueous solution of the cell material [$a^*_{\text{sol}}(\lambda)$, dotted line] and measured after acetone extraction [$a^*_{\text{ext}}(\lambda)$, dashed line].

Absorption efficiency for various phytoplankton and heterotrophic microorganisms

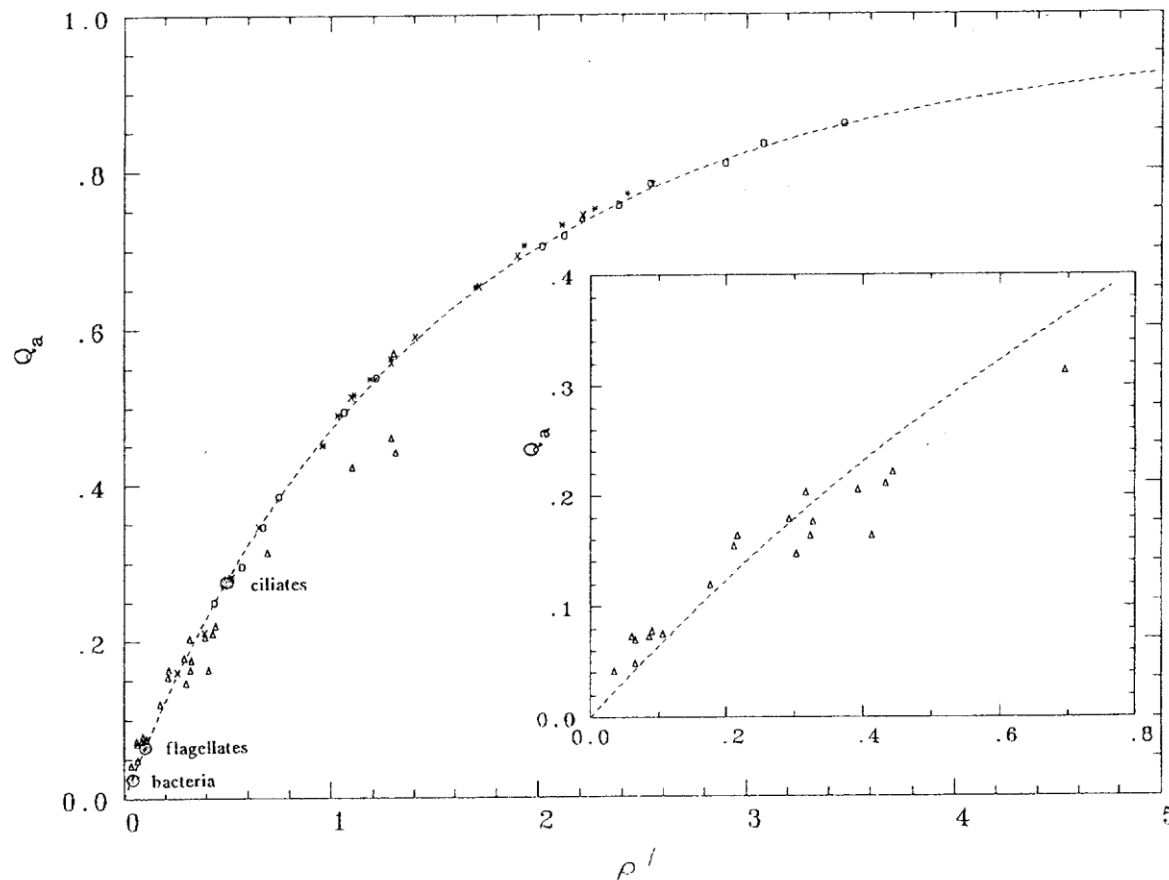


Figure 1. The theoretical variations of Q_a , the efficiency factor for absorption (dashed curves), as a function of the dimensionless parameter ρ' . The triangles are experimental determinations of Q_a (at 675 nm) for various algae (Morel and Bricaud, 1986; Ahn, 1990); other symbols are for determinations of 3 algal species studied by Sosik (1988). The values for heterotrophic organisms, as indicated, come from Morel and Ahn (1990, 1991). The inset is an enlargement of the initial part of the curve.

Example spectra of absorption efficiency factor

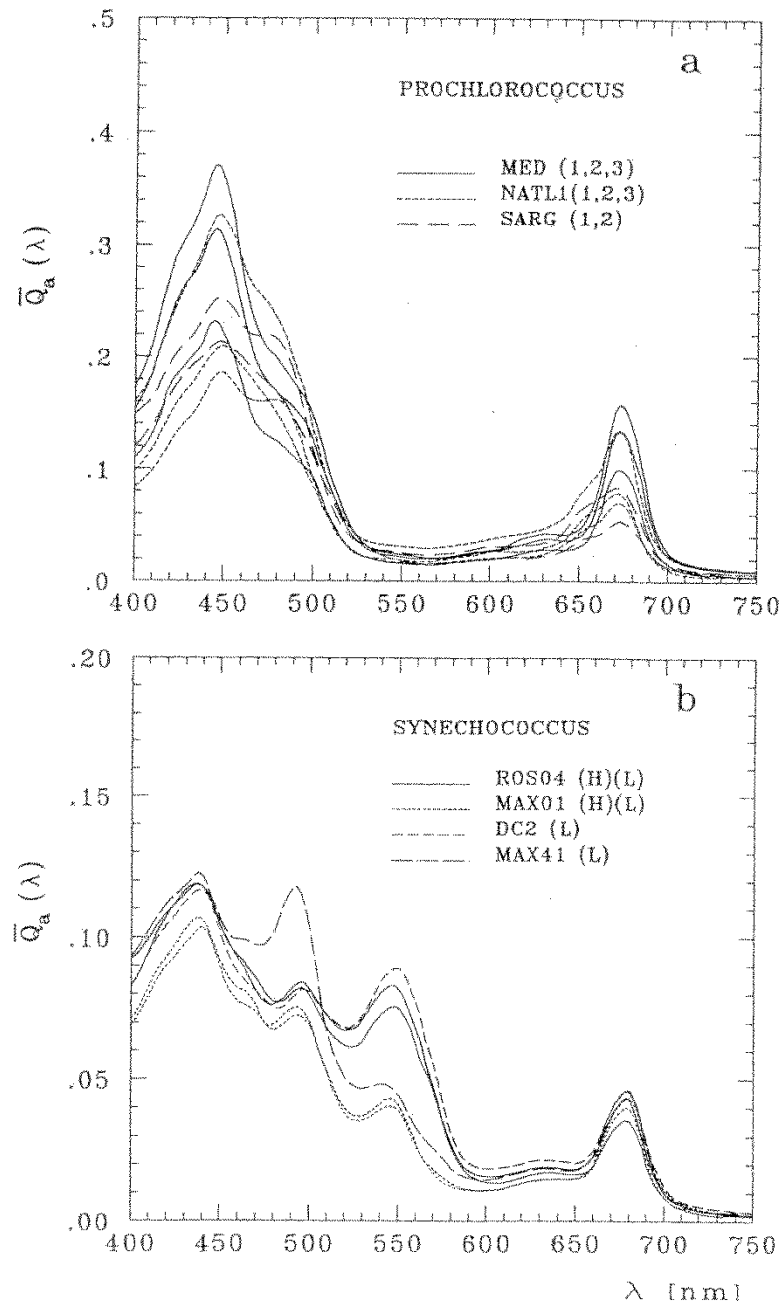


Figure 5. Spectral values of the efficiency factor for absorption for the various strains.

Particle size distributions of *Prochlorococcus* and *Synechococcus*

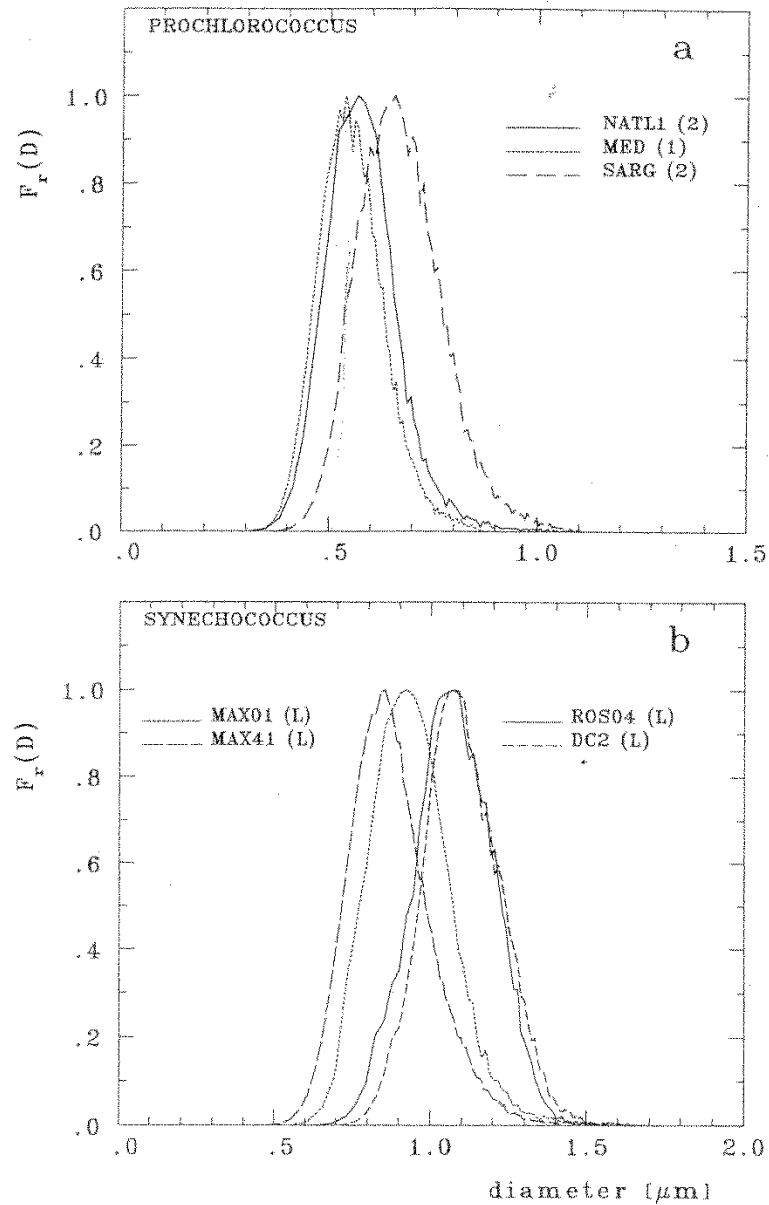
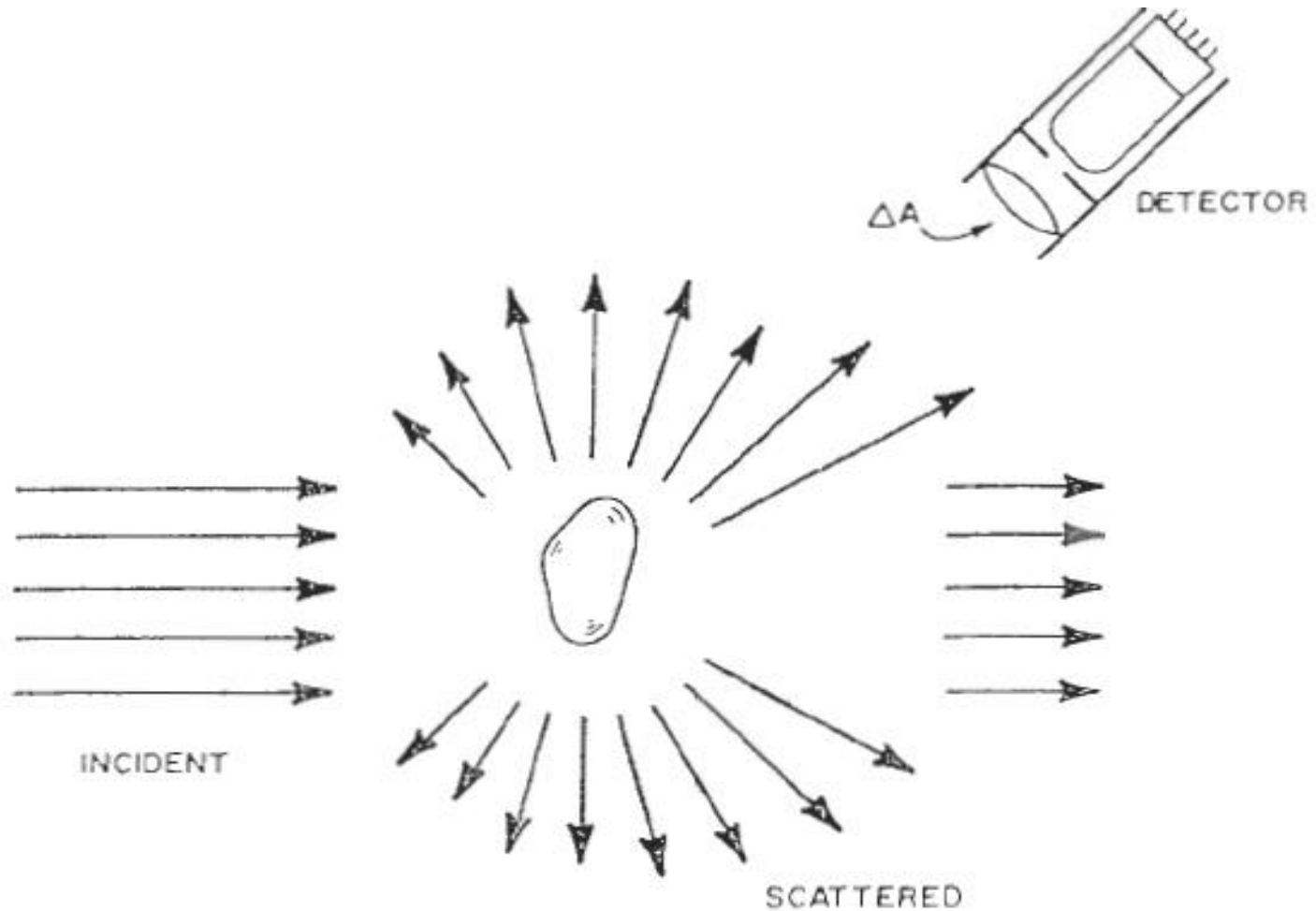
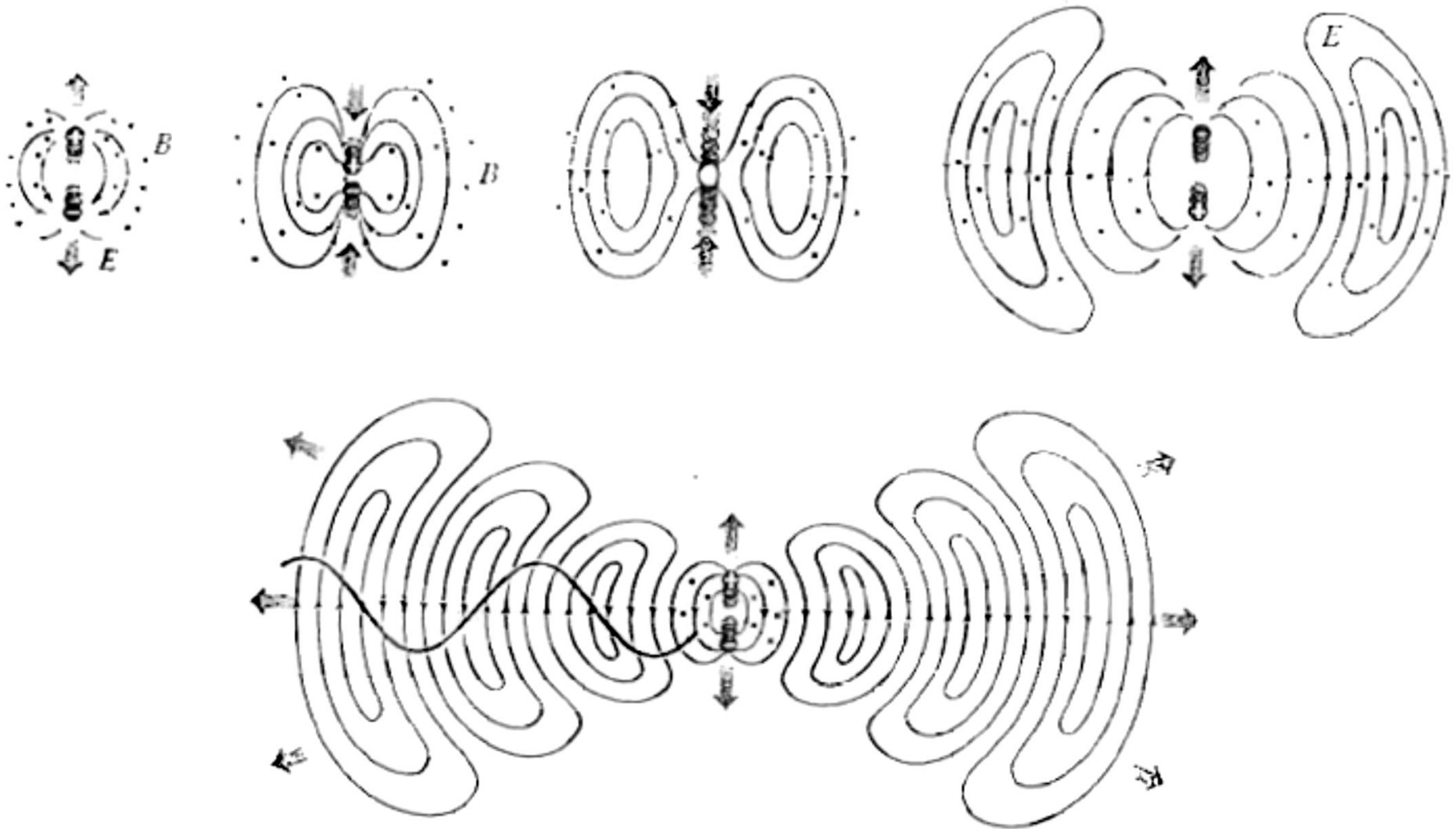


Figure 1. Relative size distribution functions (normalized to their maximum) for the various strains of *Prochlorococcus* (panel a) and *Synechococcus* (panel b), labelled as in Table 1. For clarity only one size distribution per strain is represented; the other curves, not shown, are almost identical apart from slight shifts of the maximum.

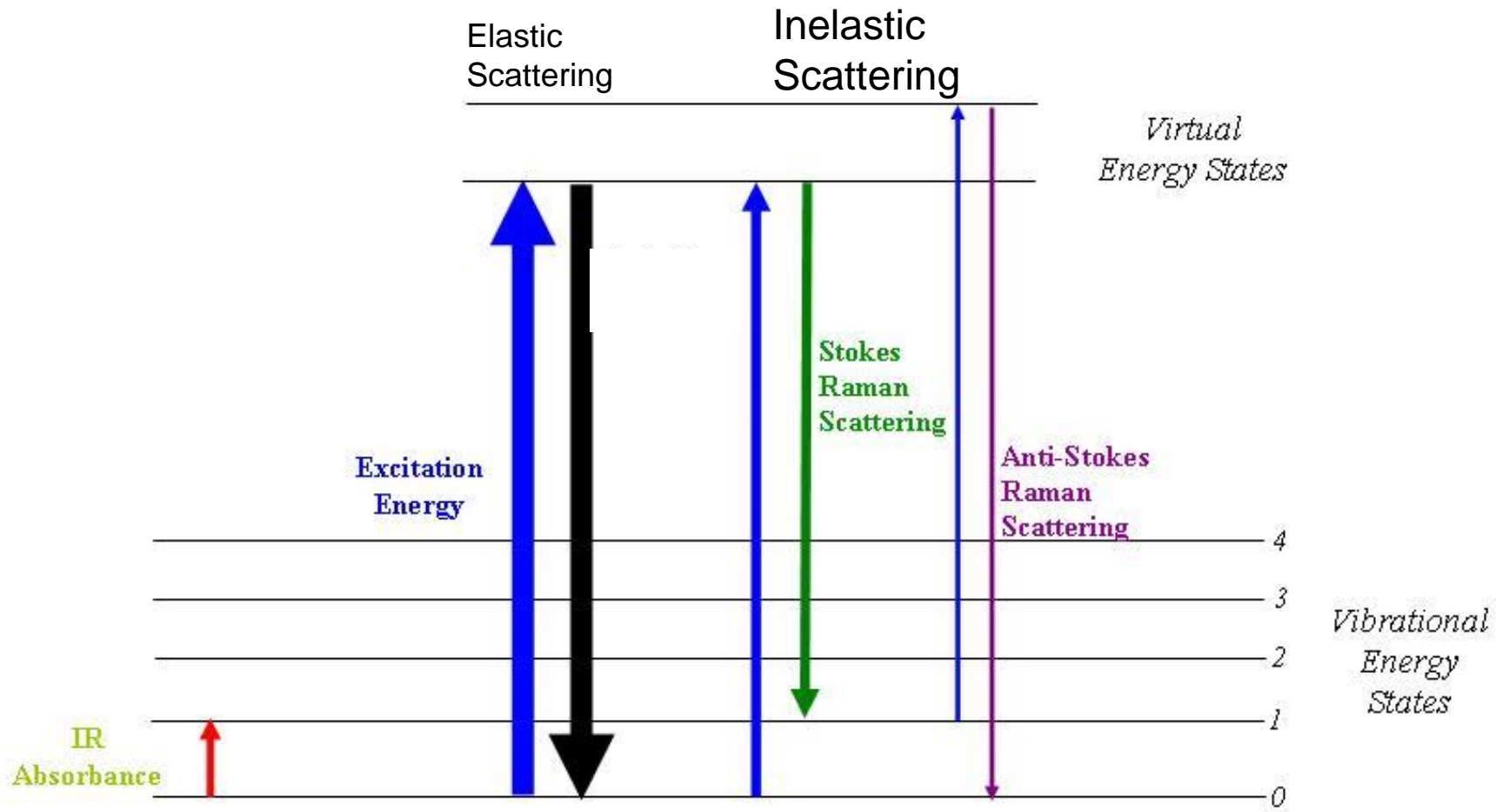
Scattering of light by inhomogeneity of the medium



Electromagnetic radiation of an oscillating dipole: Mechanism of light scattering

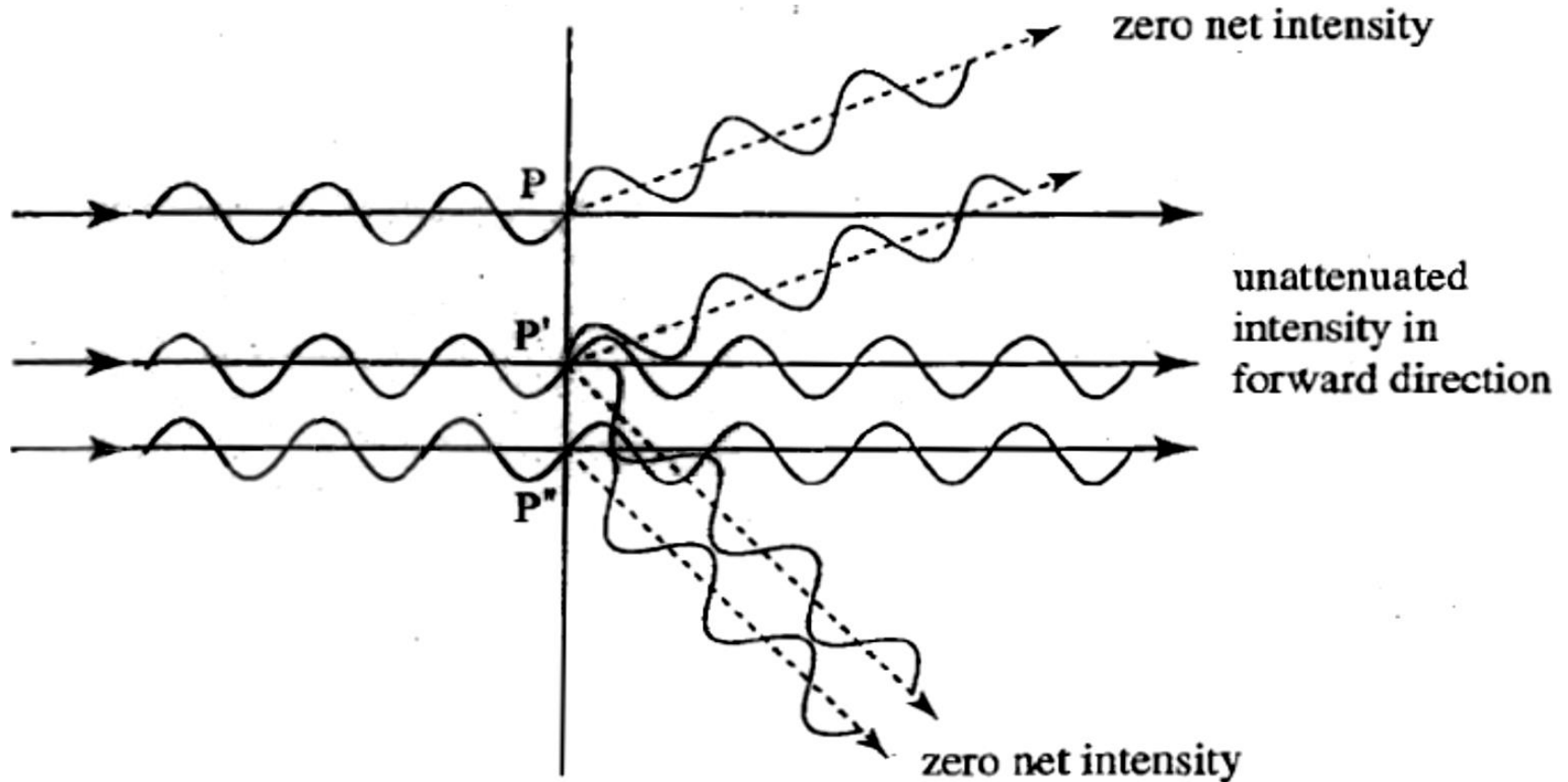


Inelastic scattering - Raman scattering

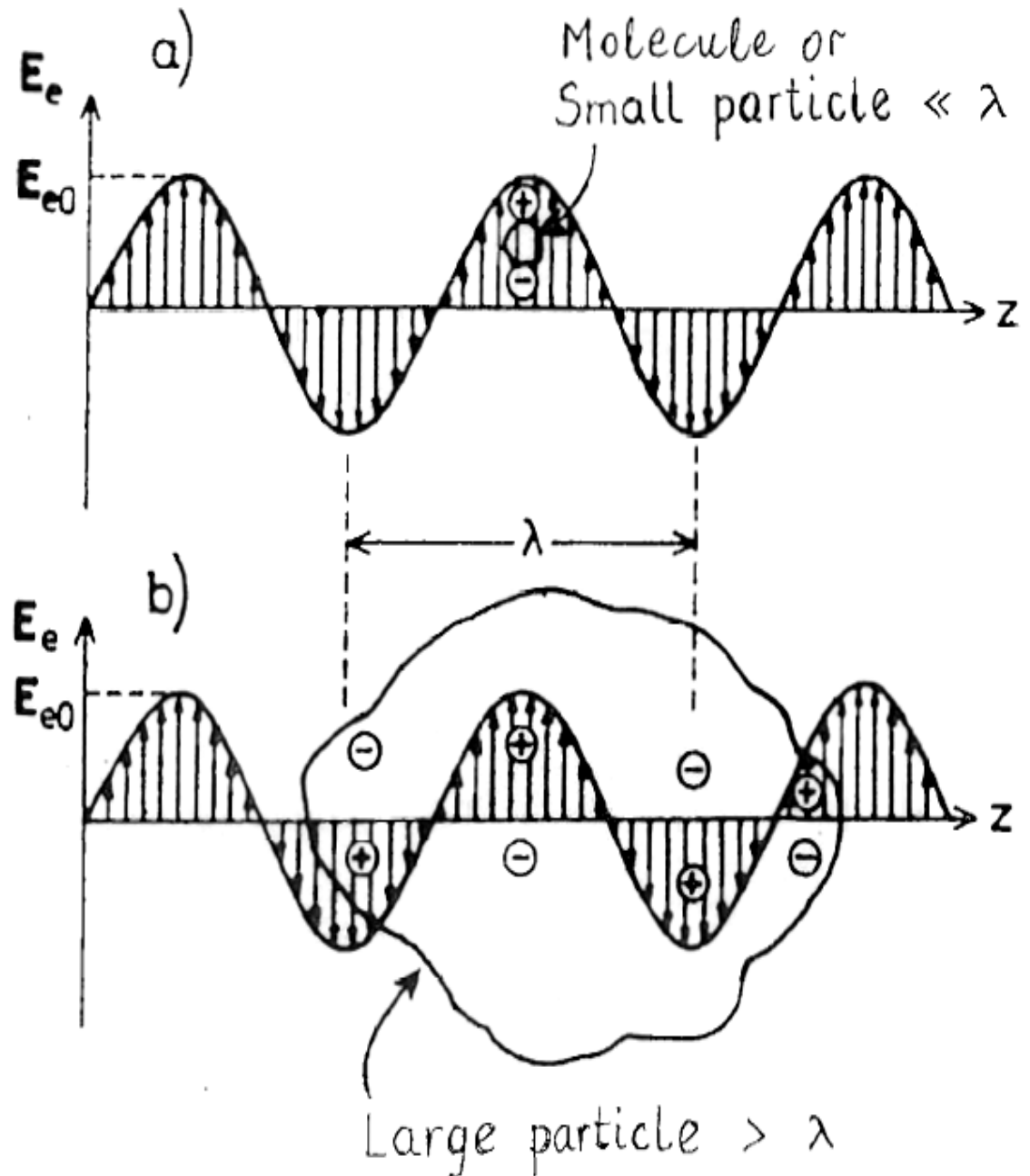


Dense homogeneous medium

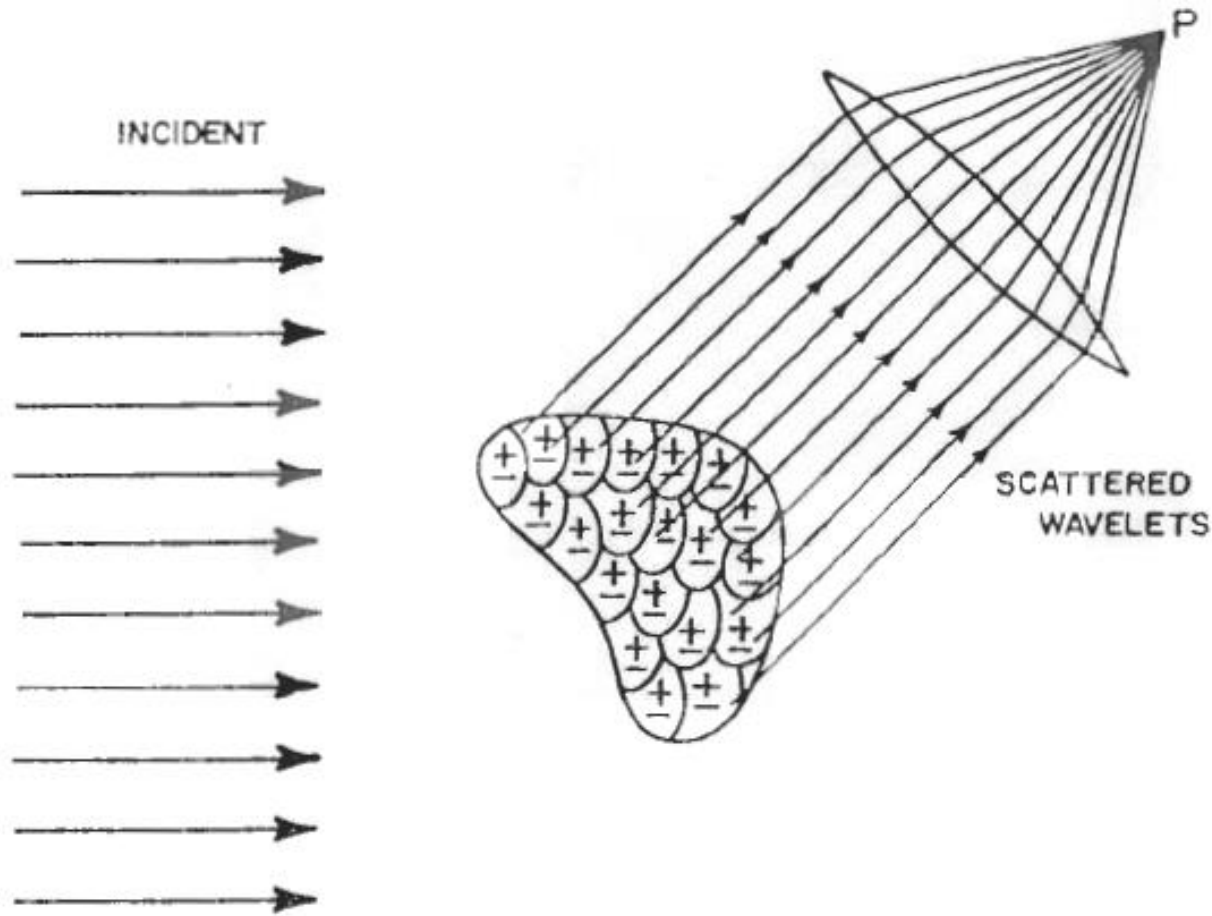
Except for forward ($\psi = 0^\circ$) and backward ($\psi = 180^\circ$) directions the scattered radiation fields are 180° out-of-phase and therefore interfere destructively



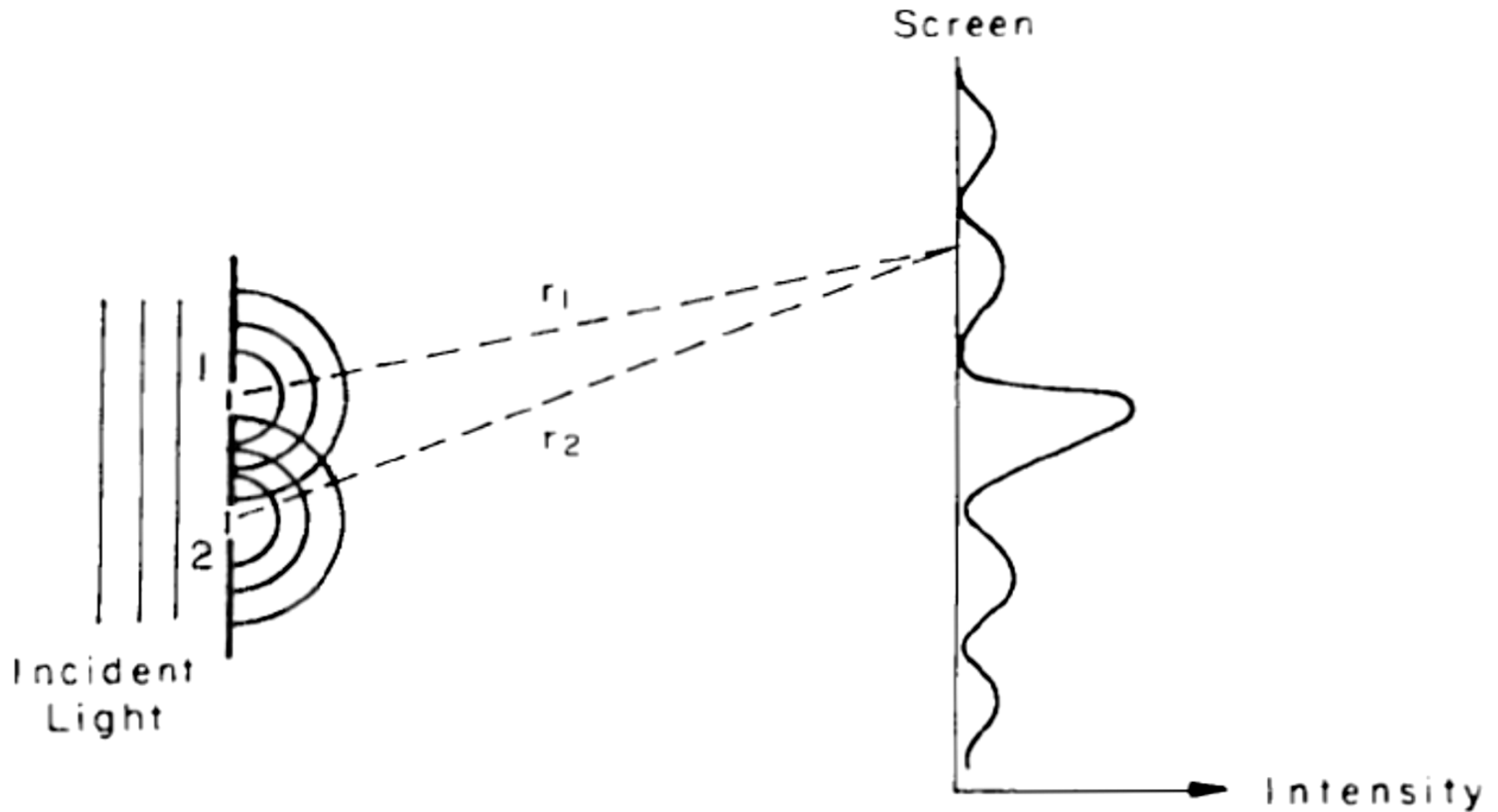
Small and large particle in the electric field of the electromagnetic wave



A single particle subdivided into oscillating dipoles



The interference pattern produced by two slits



Angular patterns of scattered intensity from particles of different sizes

Small Particles (a)



Size: smaller than one-tenth the wavelength of light
Description: symmetric

Large Particles (b)



Size: approximately one-fourth the wavelength of light
Description: scattering concentrated in forward direction

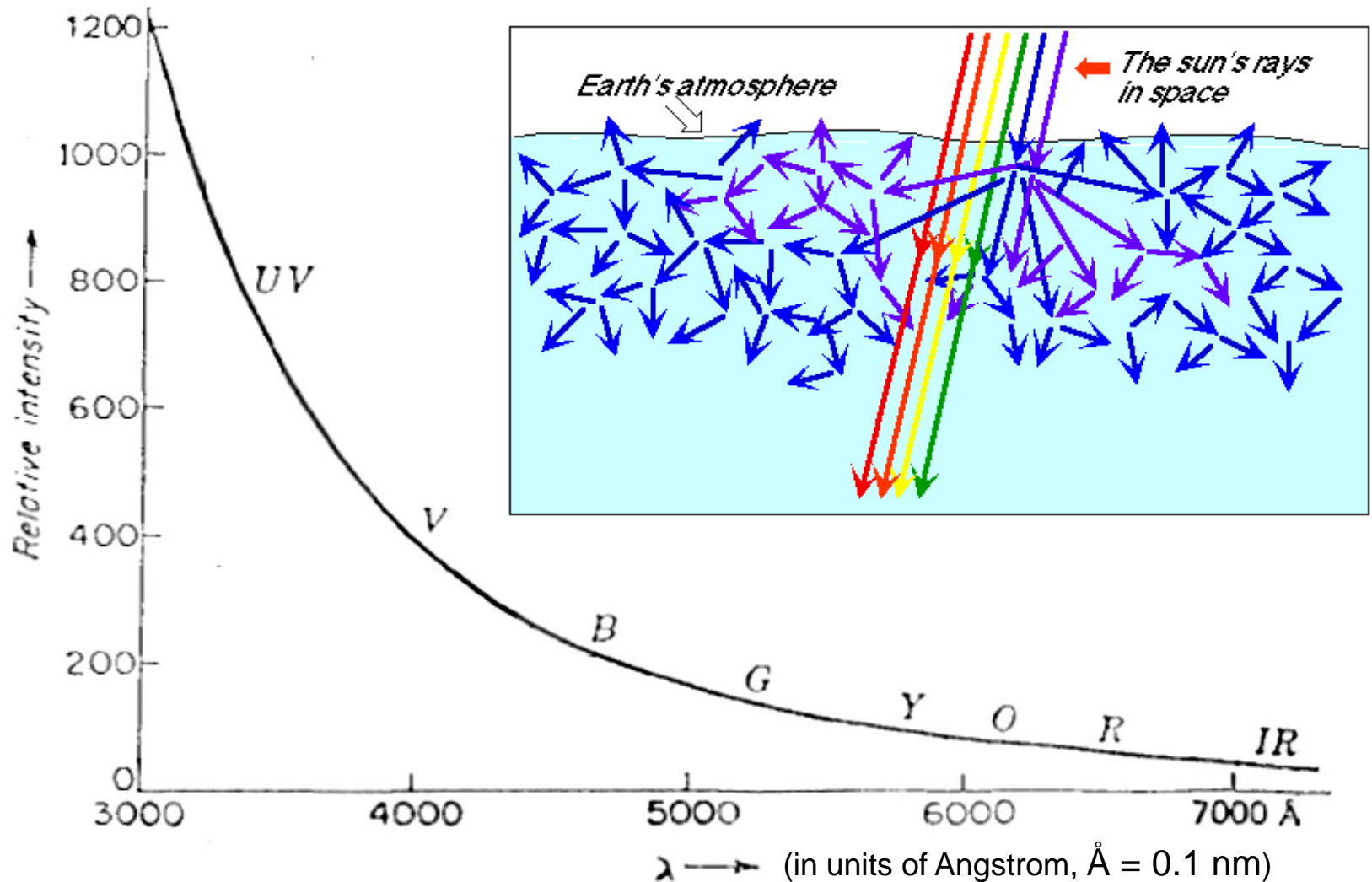
Larger Particles (c)



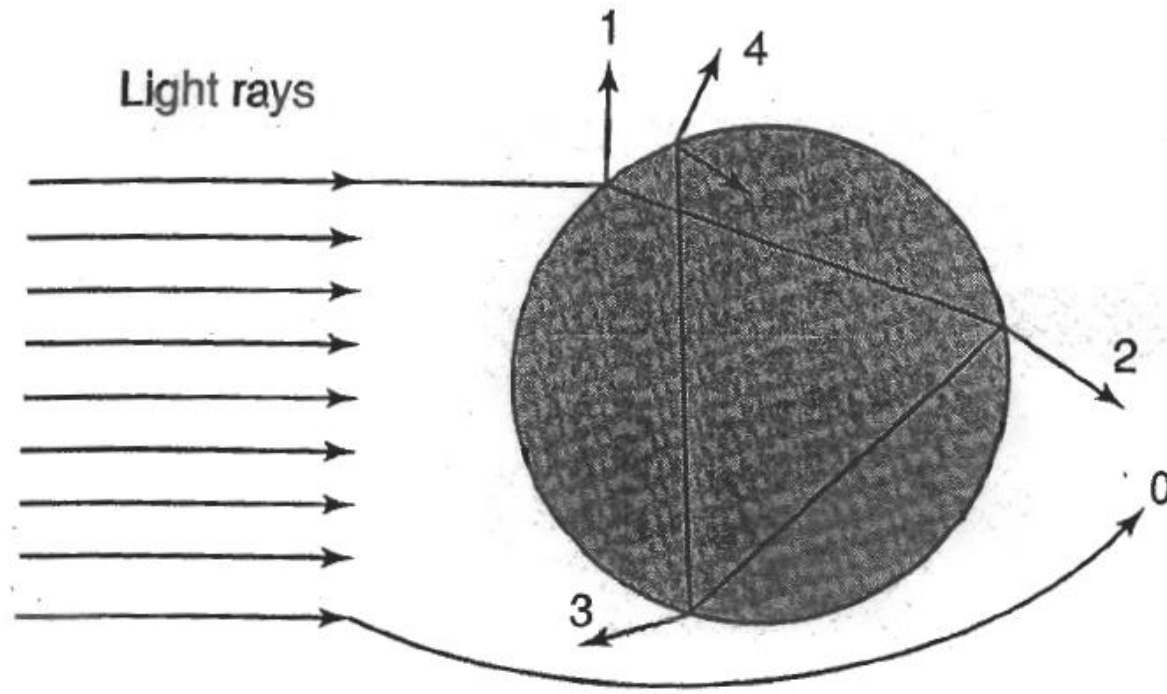
Size: larger than the wavelength of light
Description: extreme concentration of scattering in forward direction;
development of maxima and minima of scattering at wider angles

Molecular scattering as a function of light wavelength

$$\text{Scattered Intensity} \sim \lambda^{-4}$$



Geometric ray tracing approach



0 Exterior Diffraction

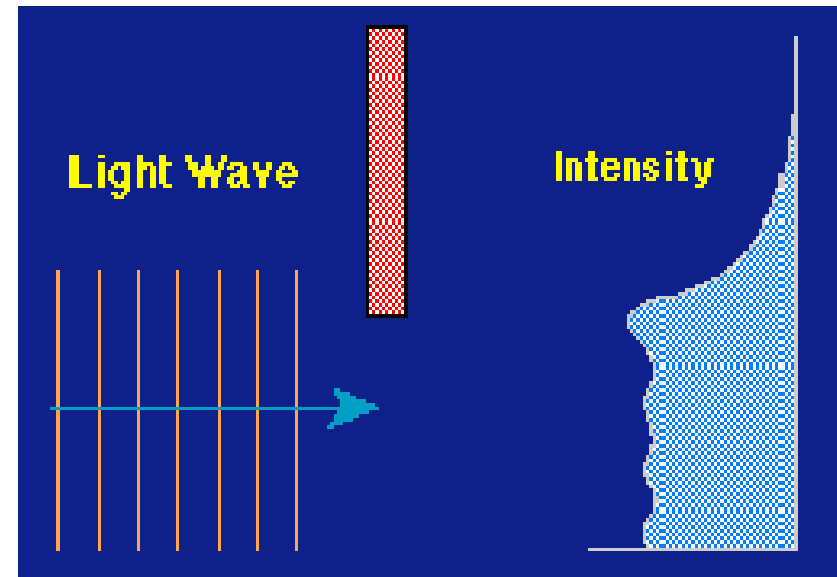
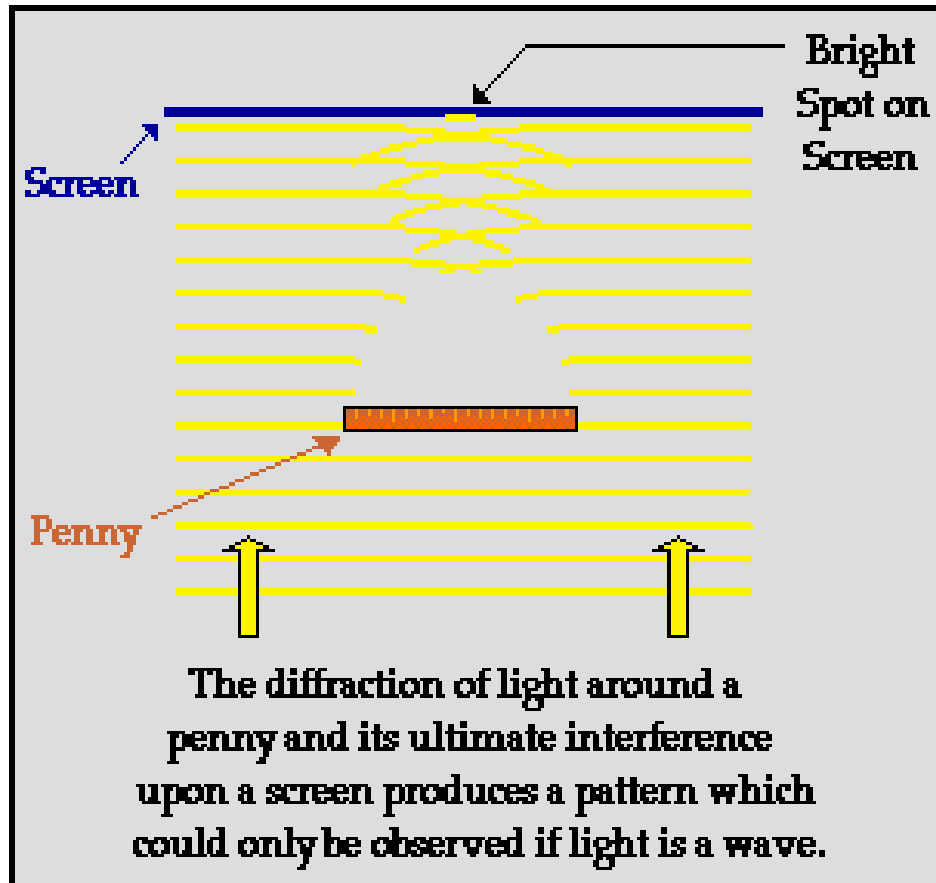
1 External Reflection

2 Two Refractions

3 One Internal Reflection

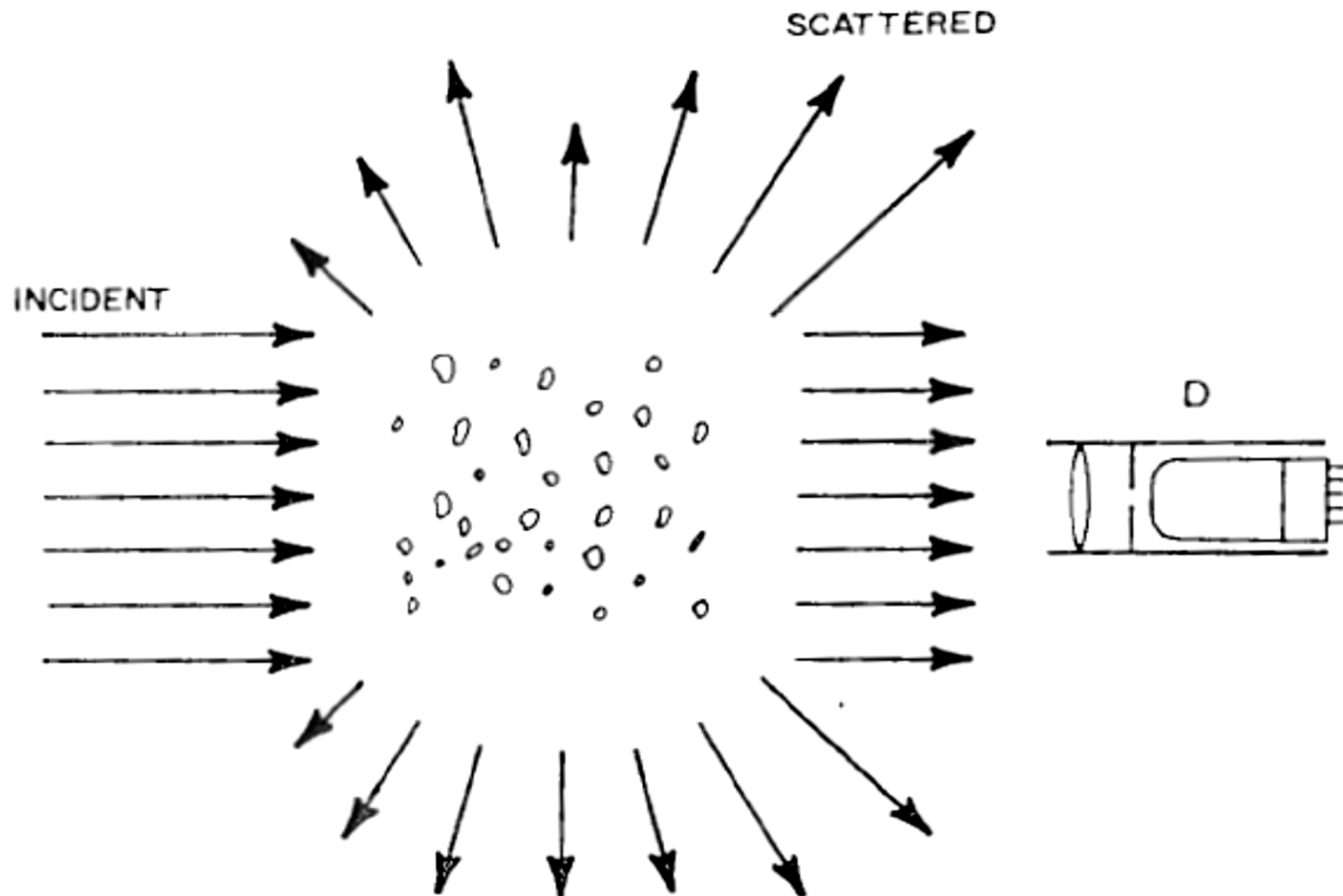
4 Two Internal Reflections

Diffraction



The intensity of light behind the barrier is not zero in the shadow region due to diffraction (light wave has a capability to “bend around corners”)

Scattering by a collection of particles



Multiple light scattering by a collection of particles

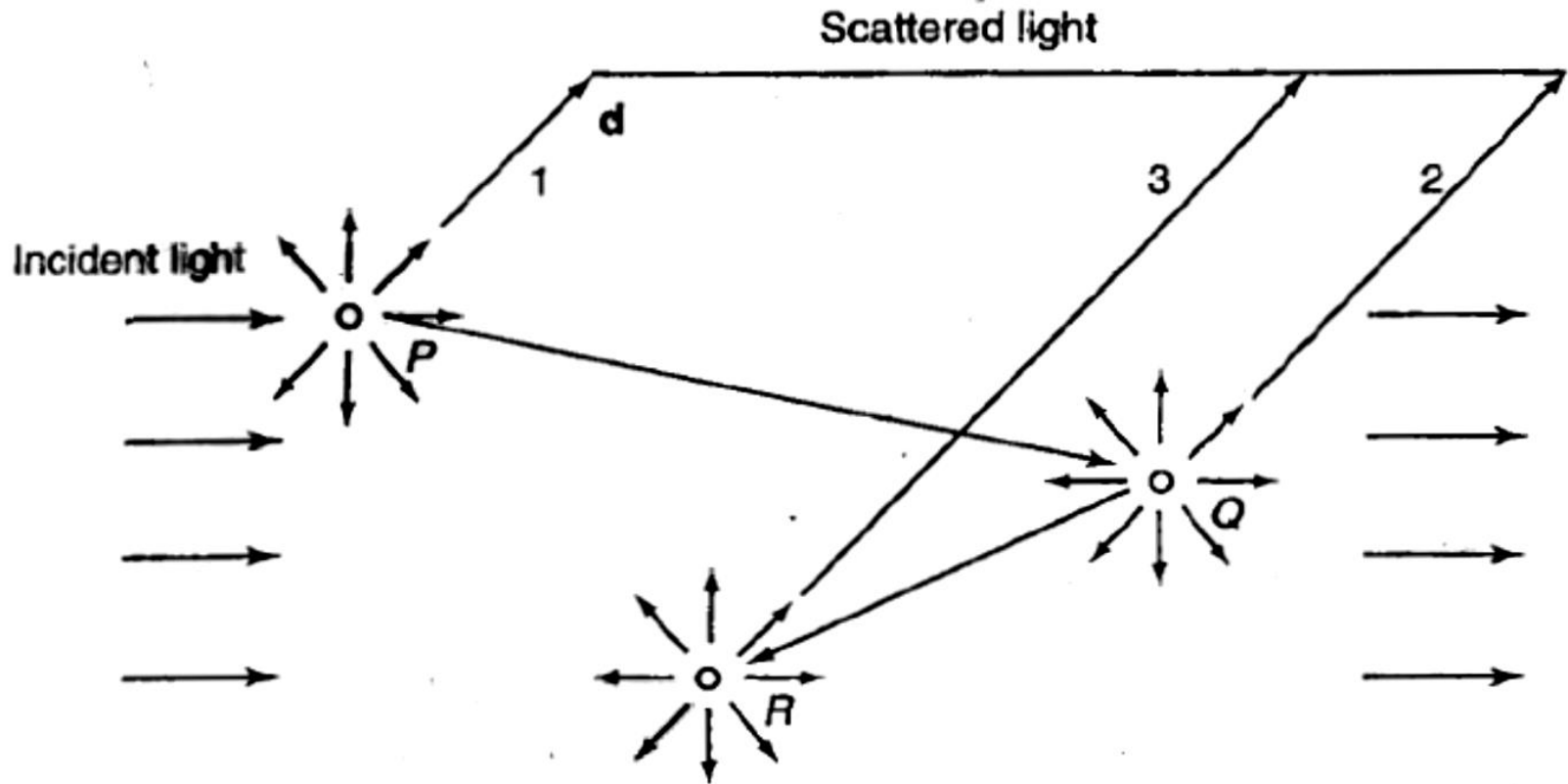


Figure 1.5 Multiple scattering process involving first (P), second (Q), and third (R) order scattering in the direction denoted by d .

Scattering by a single particle: Phase shift parameter

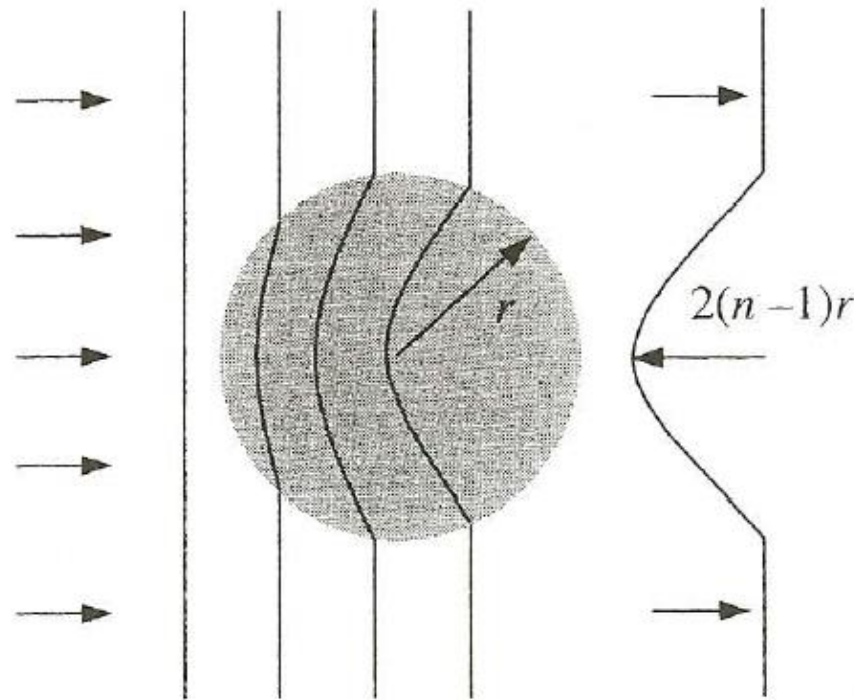


Figure 3.5. Phase fronts of a light wave traveling through a sphere of radius r . The wave slows down while traveling through the particle. The accumulated phase difference is proportional to the total distance traveled through the particle and is a function of the point of entry. The phase difference between the light passing through the center of the sphere and the light passing outside the sphere is $2(n-1)r$.

Optical efficiency factors versus phase shift parameter

phase shift parameter $\rho = 2 \alpha (n-1)$

$$Q_a = F_a/F_o$$

$$Q_b = F_b/F_o$$

$$Q_c = F_c/F_o$$

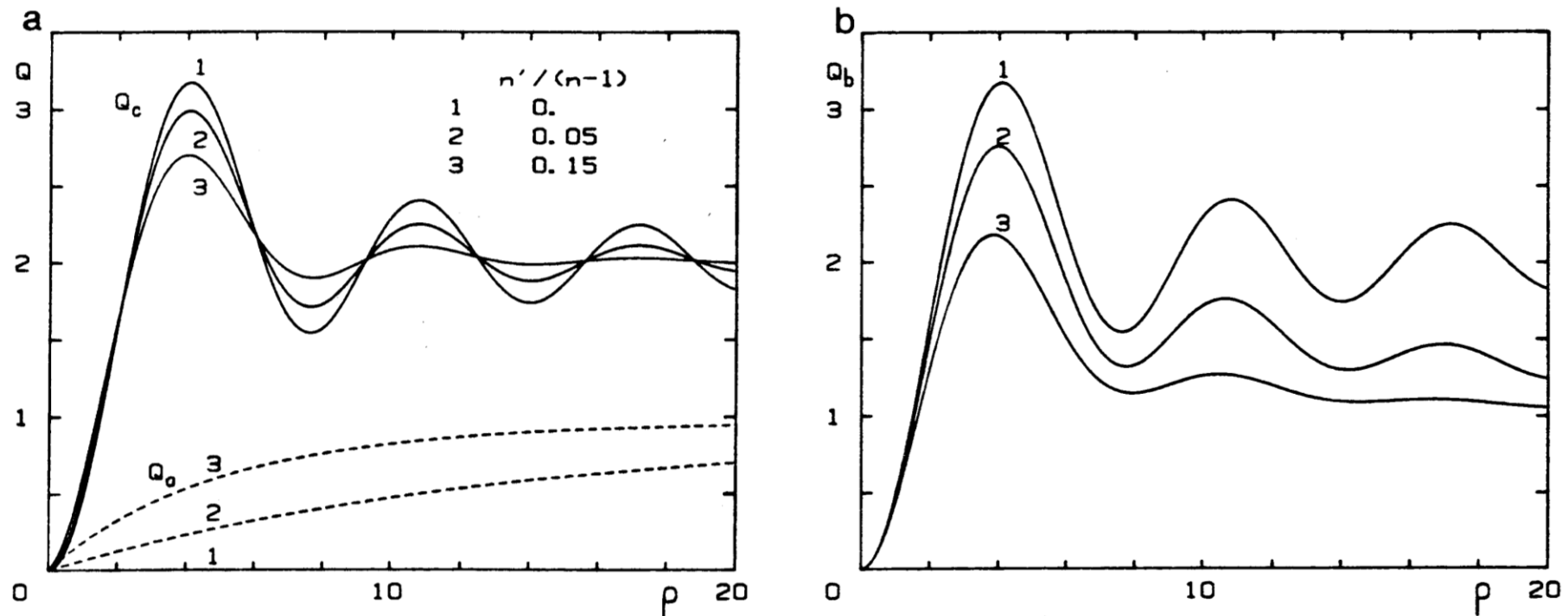


FIG. 3. Variations of the efficiency factors for attenuation, Q_c , for absorption, Q_a (a), and for scattering, Q_b (b) vs. the parameter $\rho = 2 \alpha (n-1)$, for increasing values of the ratio $n'/(n-1)$ where n and n' are the real and imaginary parts of the relative refractive index of the particles.

The effect of polydispersion on attenuation efficiency

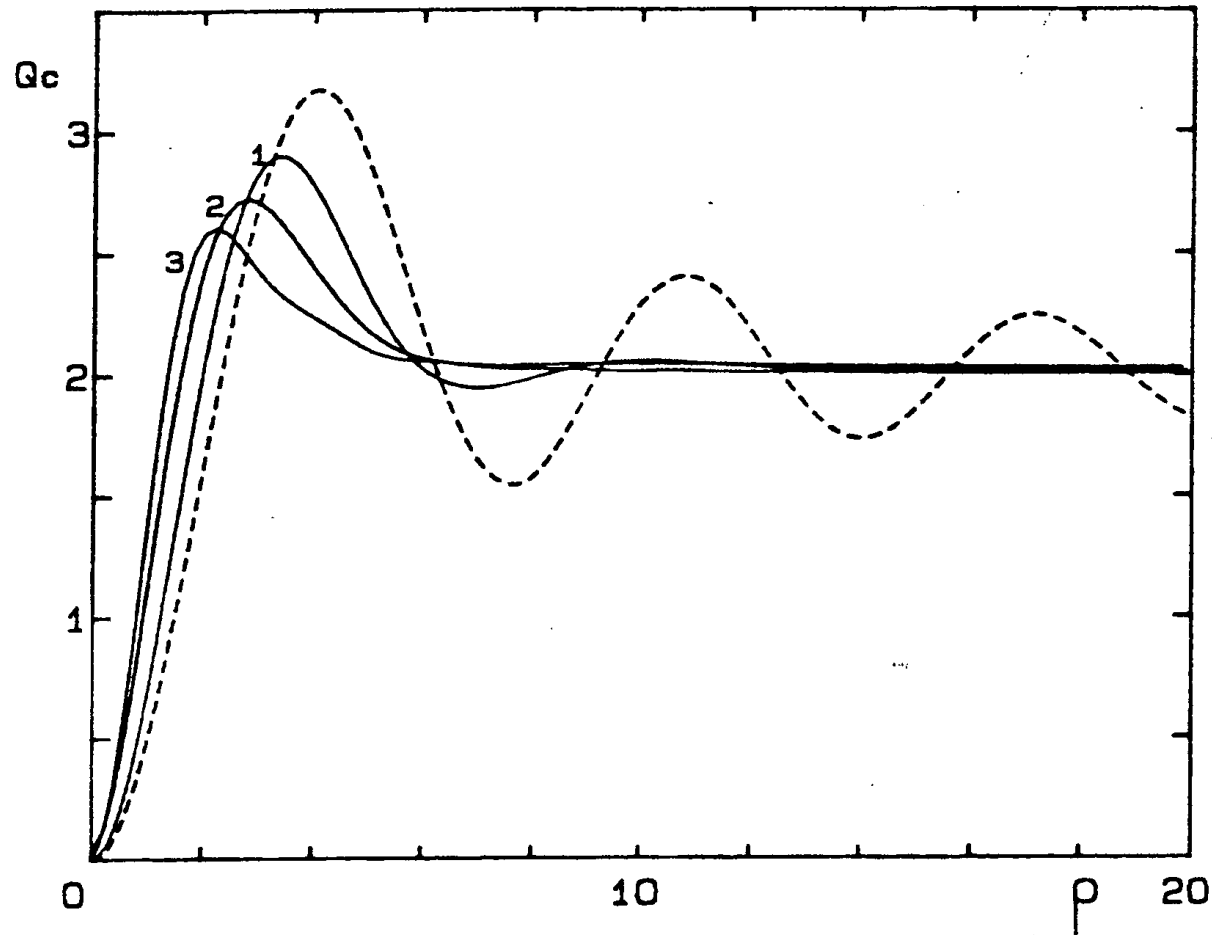
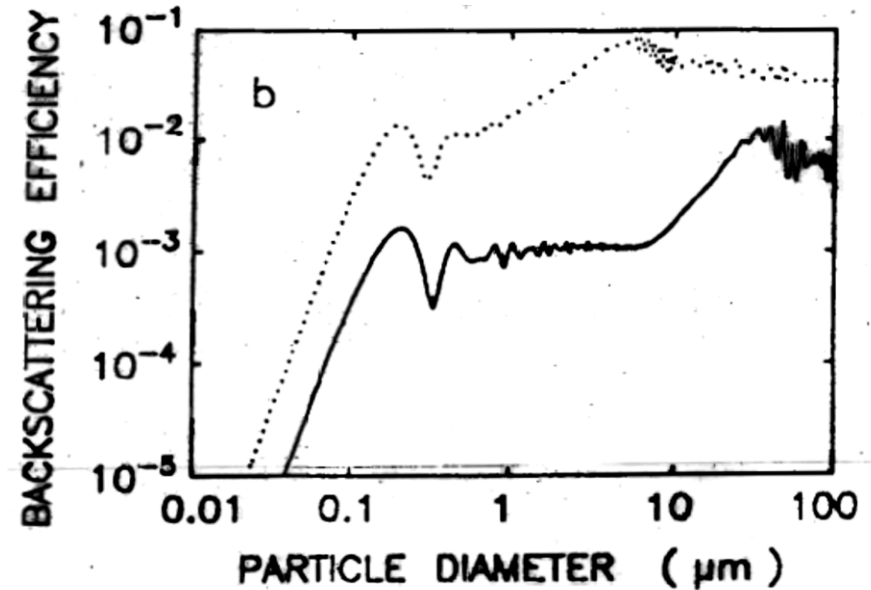
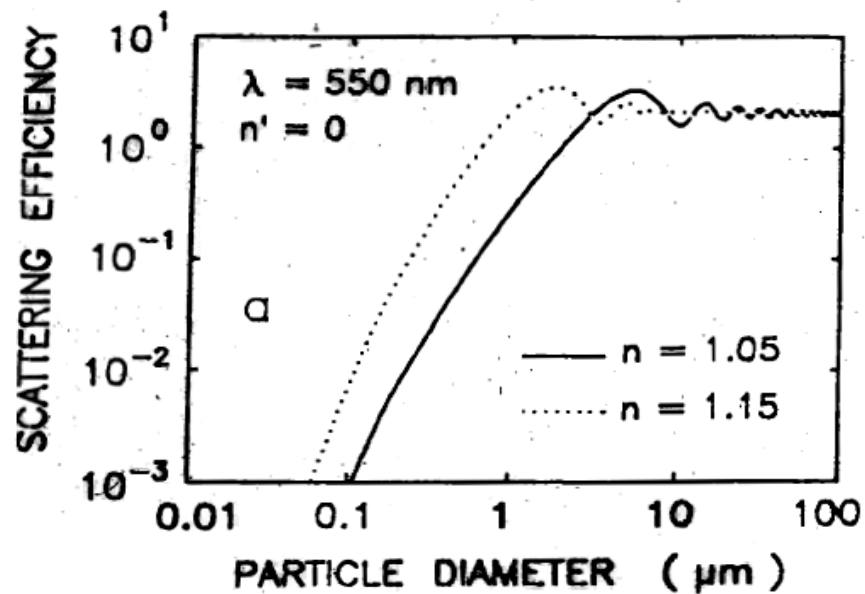


FIG. 4. Mean efficiency factor for attenuation Q_c of a “mean” particle representative of a polydisperse population, plotted as a function of ρ_m , the ρ value which corresponds to the maximum of the size distribution function $F(\rho)$ (see Equation 17). The index of refraction is real (no absorption) and the curves 1 and 3 correspond to log-normal distributions such as $F(\rho_M/2) = F(2\rho_M) =$ respectively 0.01, 0.1, 0.3 $F(\rho_M)$. The dashed curve, redrawn from Fig. 3 for $n' = 0$, represents the limiting case of a population of monosized particles.

Scattering and backscattering efficiencies versus particle size



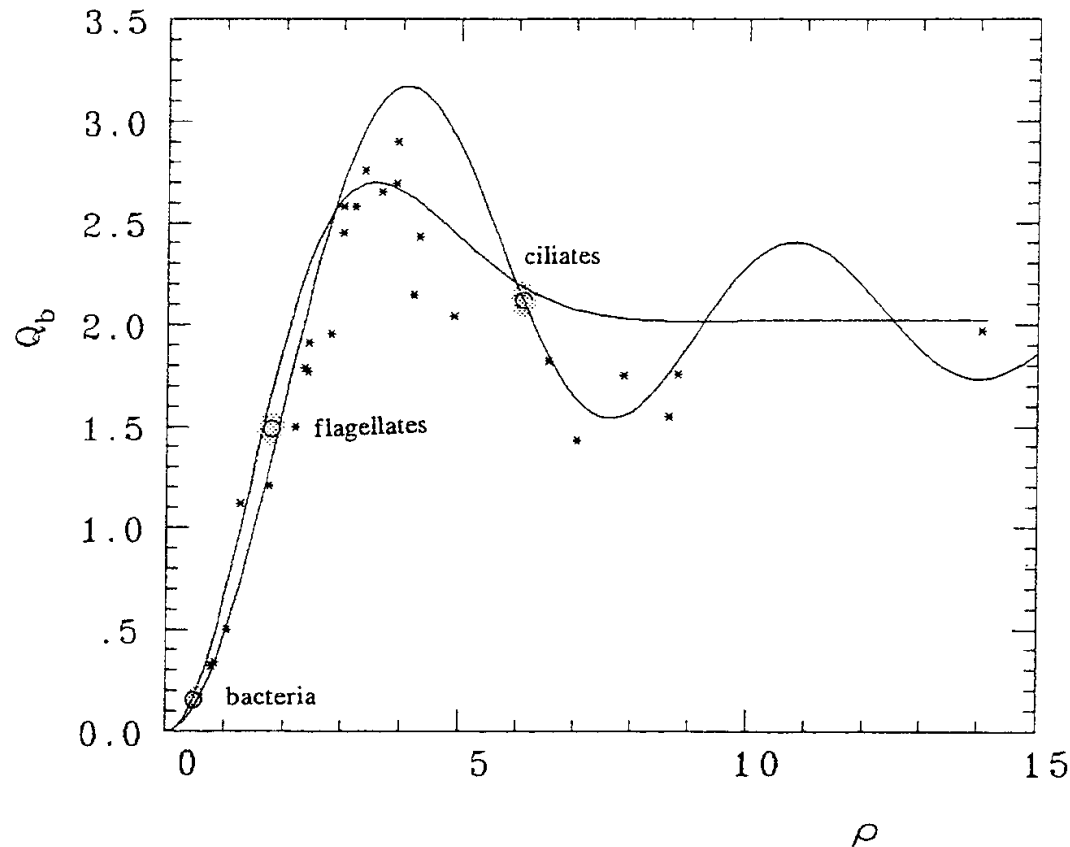


Figure 2. The theoretical variations of Q_p , the efficiency factor for scattering by non absorbing spheres (solid curve with marked oscillations) as a function of the dimensionless parameter ρ . The smoothed curve is for an averaged \bar{Q}_p to be applied for population with a log - normal size distribution. The crosses are the \bar{Q}_p values (at $\lambda \sim 580$ nm) determined for various phytoplankters grown in culture (see Table 1 in Morel and Bricaud, 1986); additional data for algal cells come from Ahn (1990). The circles indicate the \bar{Q}_p values (at $\lambda \sim 550$ nm) determined for free living marine bacteria, heterotrophic flagellates, and naked ciliates, (Morel and Ahn, 1990; 1991).

Spectra of scattering efficiency for various phototrophic and heterotrophic microorganisms

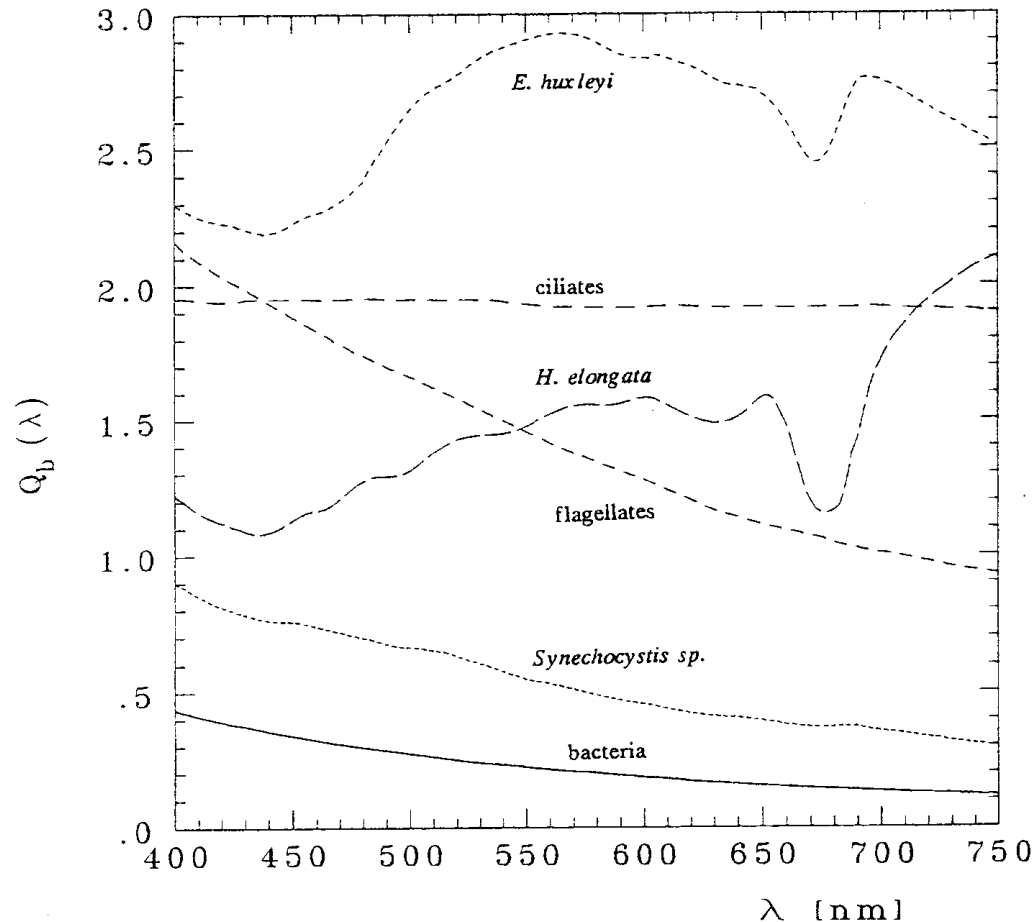
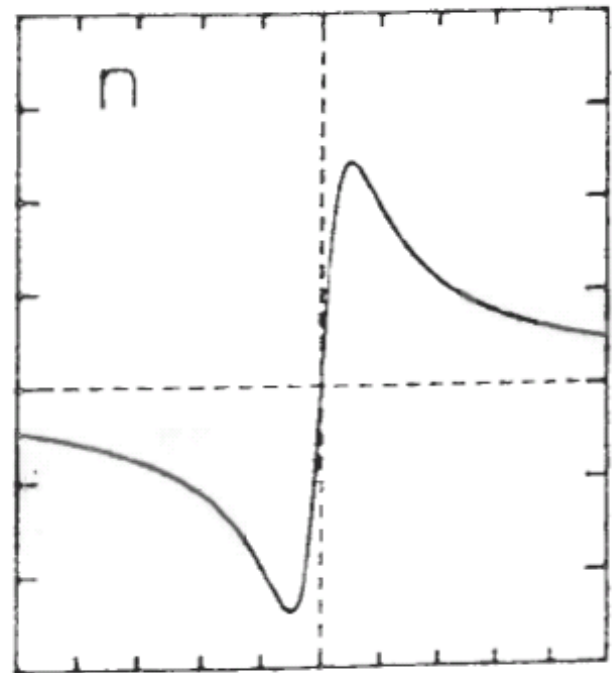
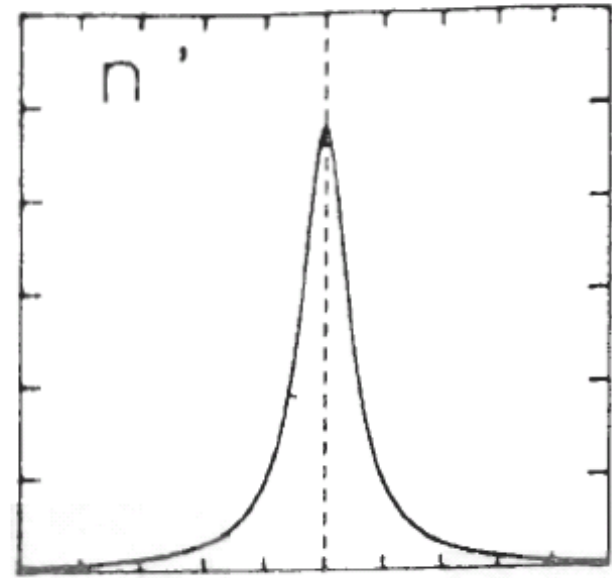


Figure 3. Spectral variations of Q_b within the 400-750 nm range of various phototrophic and heterotrophic organisms as experimentally determined (Morel and Ahn, 1990, 1991).

Anomalous dispersion of the refractive index within the absorption band



Optical efficiency factors:
 Examples for monospecific
 cultures of algal cells
 (deduced from the absorption
 and attenuation coefficients,
 and size distribution
 measurements)

$\bar{d} = 3.4 \mu\text{m}$
 $n \approx 1.07$
 $\alpha \approx 20 \dots 35$
 $\beta \approx 3 \dots 5$
 for the visible
 light

$\bar{d} = 1.2 \mu\text{m}$
 $n \approx 1.05$
 $\alpha \approx 7 \dots 13$
 $\beta \approx 0.5 \dots 1.5$
 for the visible
 light

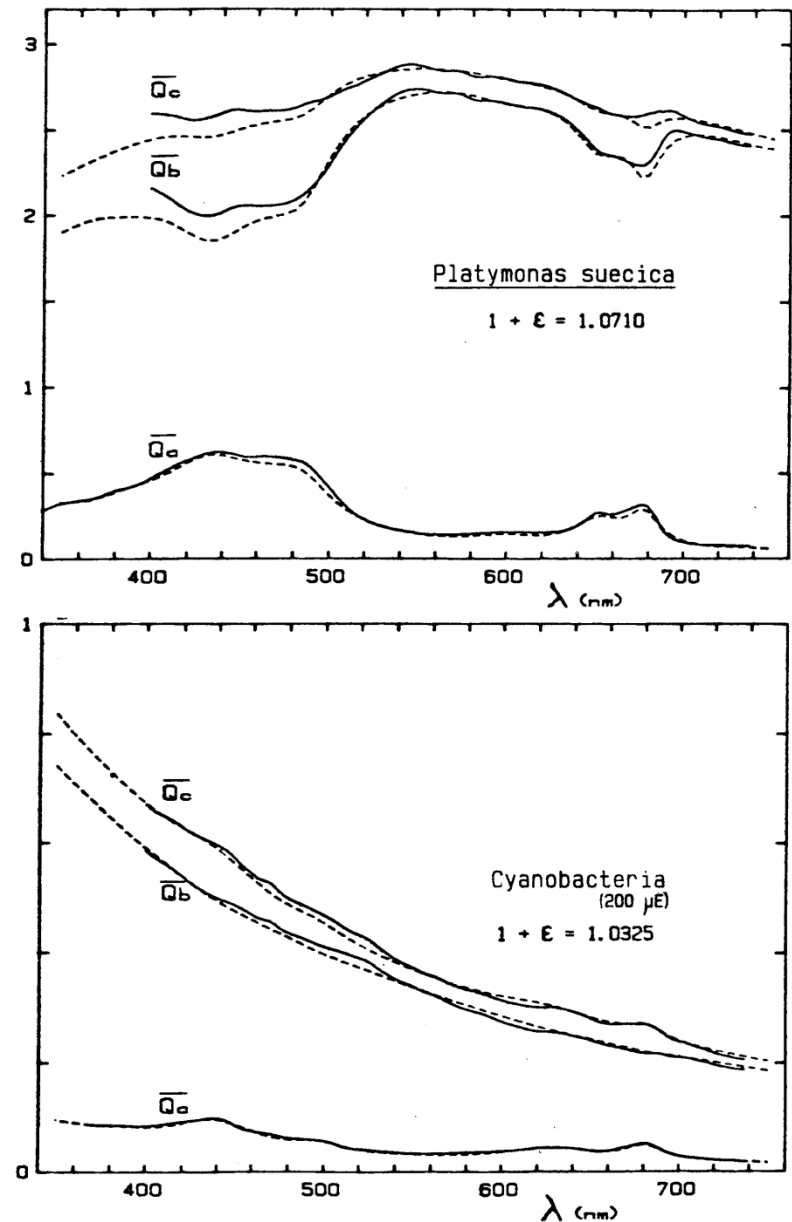


FIG. 14. Spectral variations of the mean efficiency factors for attenuation (\bar{Q}_c), scattering (\bar{Q}_b) and absorption (\bar{Q}_a), deduced from the attenuation and absorption coefficients experimentally determined (continuous lines), for two phytoplanktonic species. The variations of \bar{Q}_c , \bar{Q}_b and \bar{Q}_a obtained from a theoretical model (see text) are shown as dashed lines. The central value of the real part of the refractive index, $1 + \epsilon$, leading to the best theory/experiment agreement is indicated on the Figures.

Scattering phase function: Effect of polydispersion

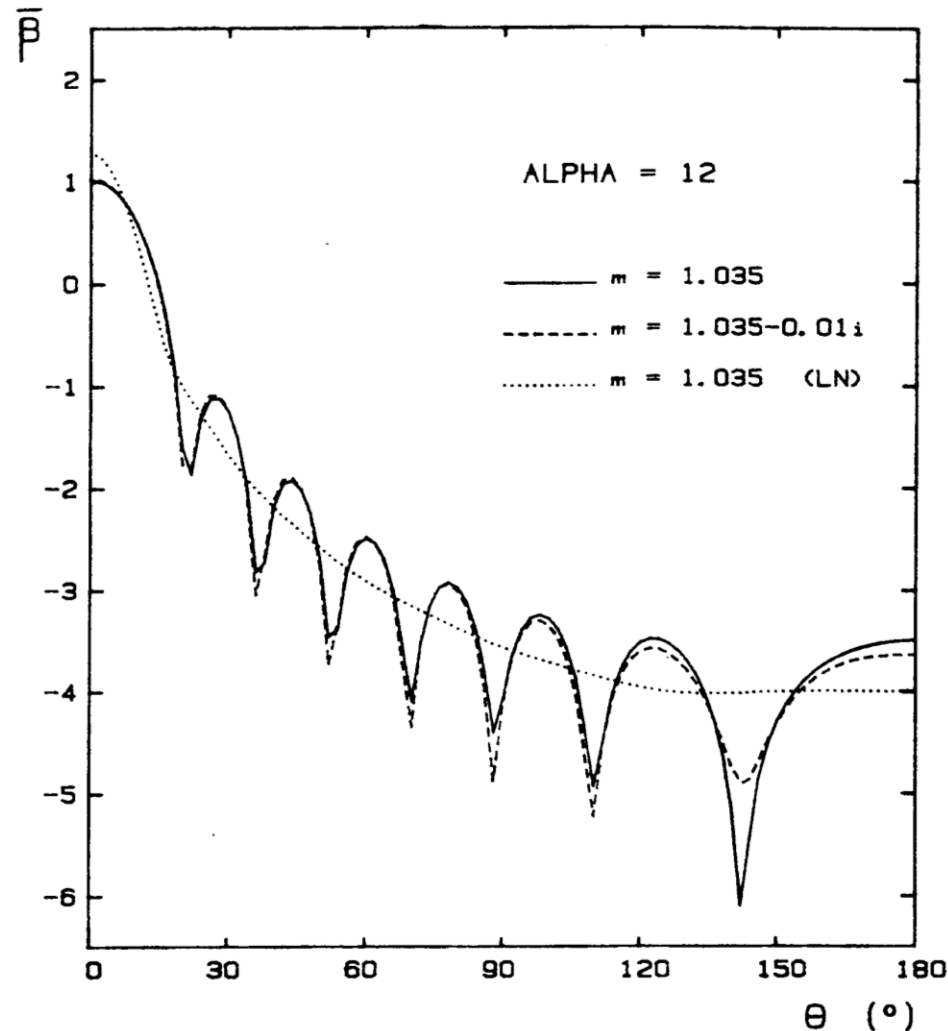


FIG. 5. Normalized volume scattering functions, $\bar{\beta}(\theta)$ (Equations 5' and 18), for a particle of relative size $\alpha = 12$, when the refractive index is 1.035 and $1.035 - 0.01i$. The dotted curve represents the same $\bar{\beta}(\theta)$ function for a polydispersed population of particles with $n = 1.035$, computed according to Equation 20. The size distribution function $F(\alpha)$ is a log-normal law such that the modal relative size $\bar{\alpha}_M$ is also 12, and $F(\alpha_M/2) = F(2\alpha_M) = 0.01 F(\alpha_M)$.

Scattering phase function: Effects of particle size and refractive index

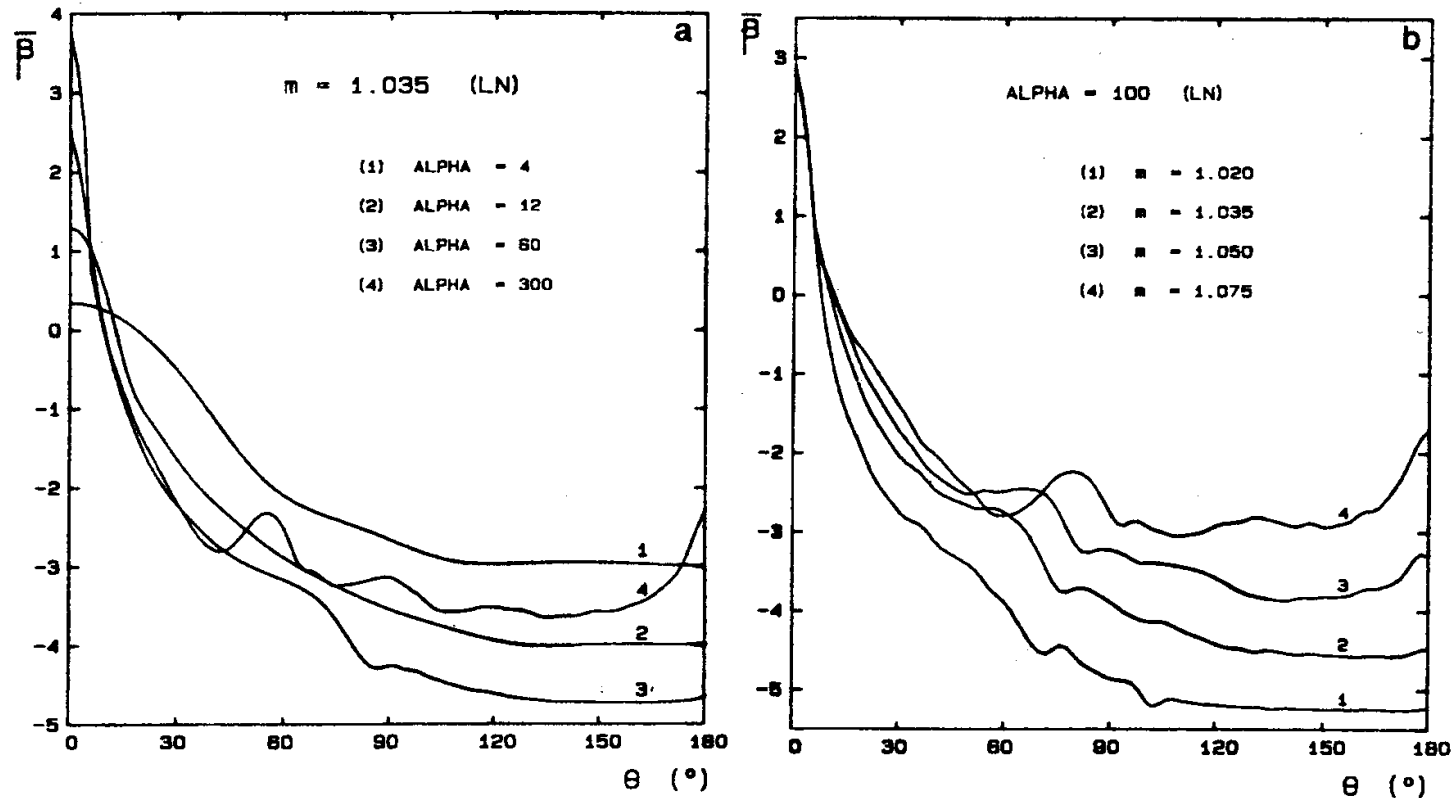


FIG. 6. (a) Normalized volume scattering function $\bar{\beta}(\theta)$ for increasing α_M values (increasing size) and for $m = 1.035$. (b) Normalized volume scattering function $\bar{\beta}(\theta)$ for increasing (real) index of refraction and for $\alpha_M = 100$. For Fig. 6a and b the log normal size distribution used is as in Fig. 5. The “bump” which occurs at about 75° for $m = 1.075$ and at smaller angles when the refractive index decreases (see also Fig. 6a) is the first “rainbow”, at 138° for water droplets ($n = 1.33$). It appears for sufficiently large and perfect spheres. Thus it is unlikely that it can be observed for algal cells.

Normalized scattering function for various microorganisms (from Mie calculations)

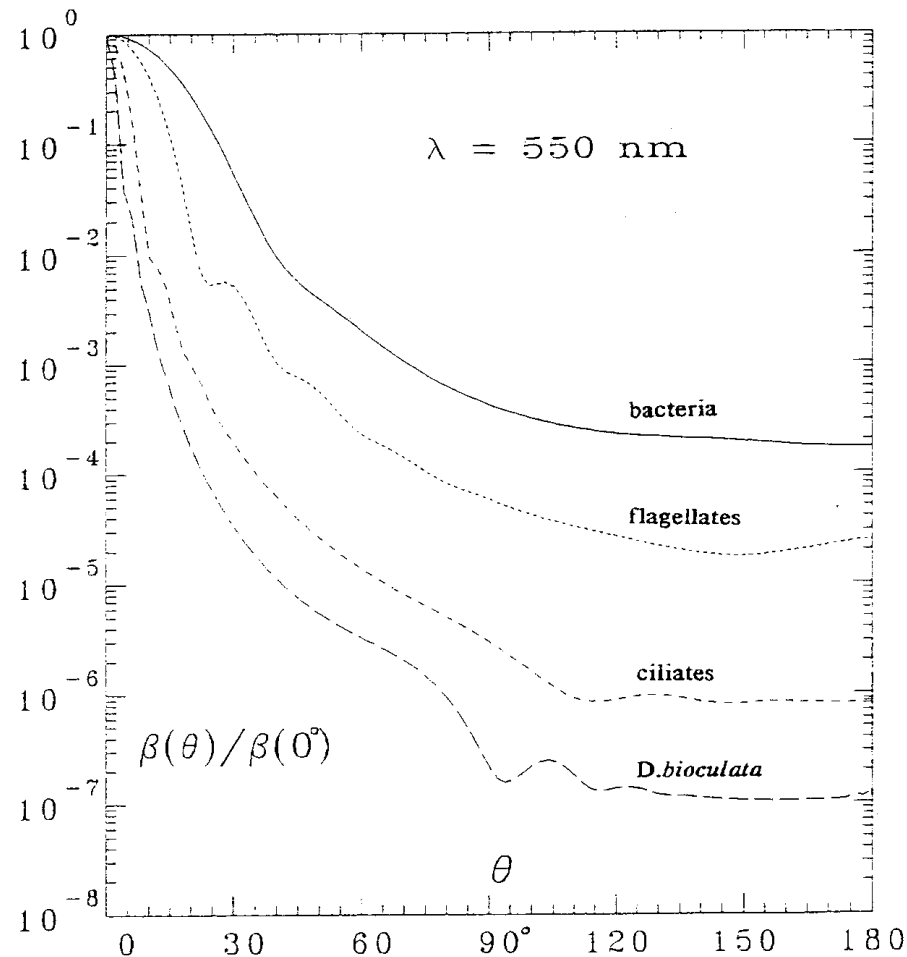


Figure 6. Volume scattering function (normalized at $\theta = 0^\circ$ and for $\lambda = 550 \text{ nm}$) computed for various organisms by using their refractive index and size distribution as experimentally determined (see text).

Backscattering ratio versus relative size parameter

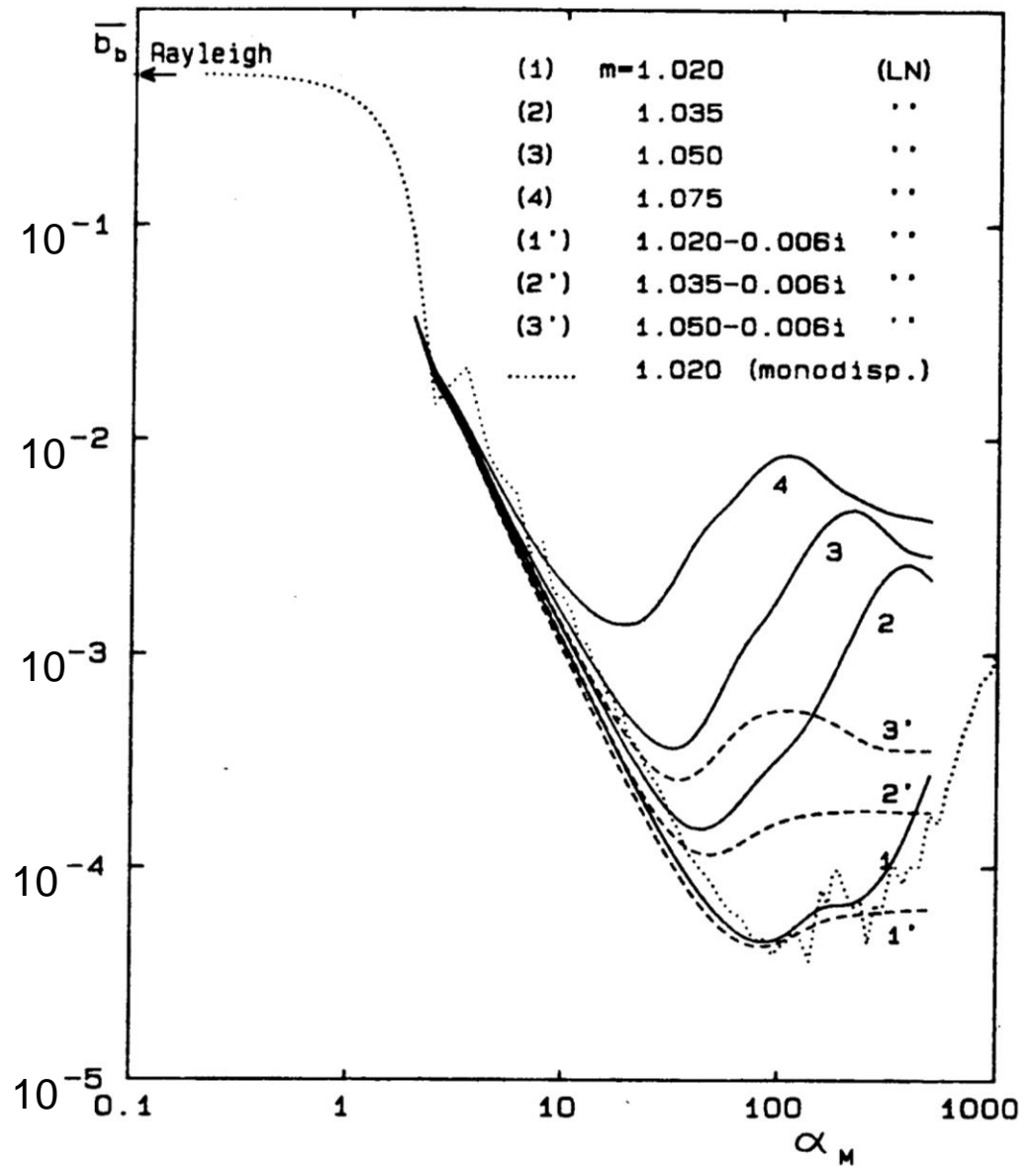
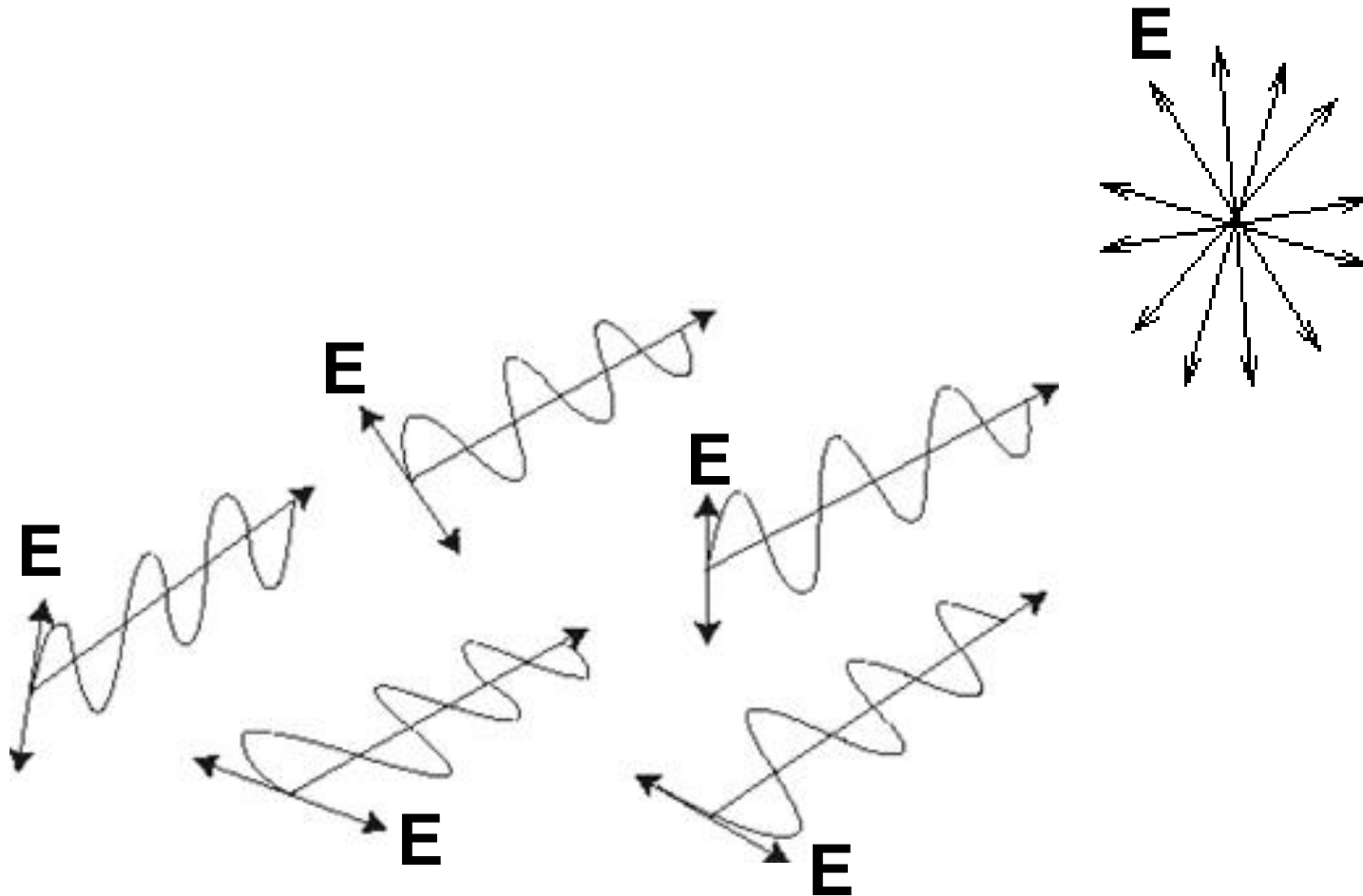
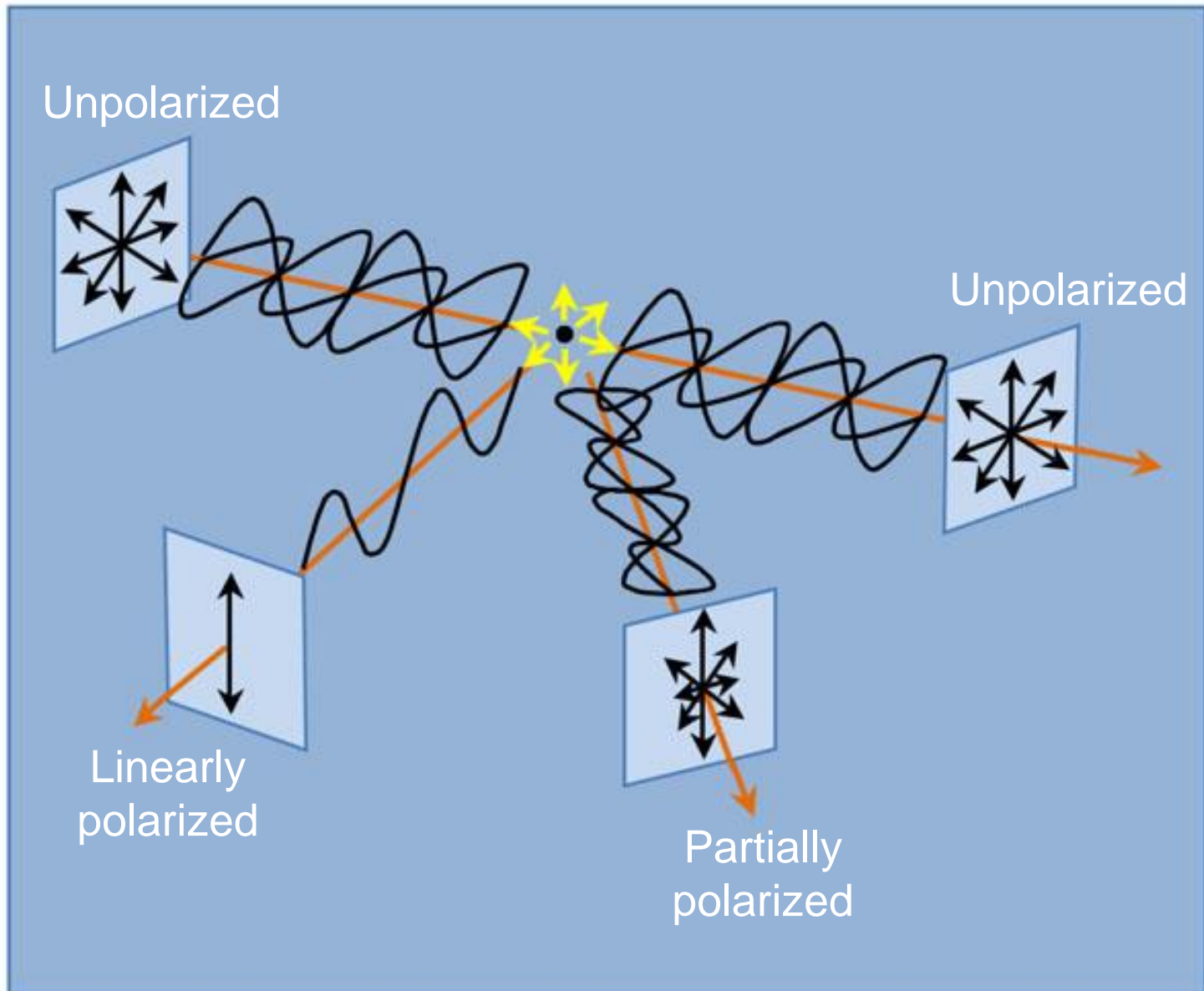


FIG. 8. Variations of the backscattering ratio $\bar{b}_b (= b_b/b)$ vs. the modal relative size α_M (same log-normal law as before in Fig. 5). The different curves correspond to various values of the refractive index given in inset. The curve for a monodispersed population (with $m = 1.02$) is also shown (dotted line). The arrow indicates the limiting value of $b_b/b (= 0.5)$ when α tends toward 0 (Rayleigh domain).

Randomly polarized (unpolarized) light is a jumble
of random, rapidly changing **E**-fields



Polarization by scattering



Scattering budget in terms of particle size fractions

Low-index particles

CONTRIBUTION TO SCATTERING BY VARIOUS SIZE CLASSES

MIE SOLUTIONS FOR

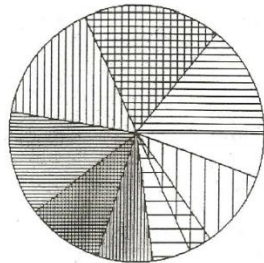
$\lambda = 550 \text{ nm}$

$n = 1.05$ (living microorganisms)

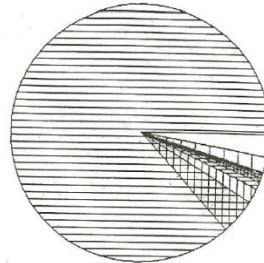
$n' = 0$

$F(D) \sim D^{-4}$

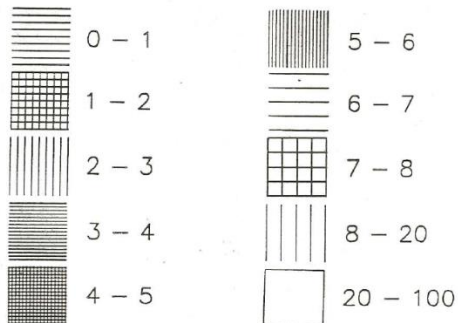
TOTAL SCATTERING



BACKSCATTERING



Size classes in micrometers



High-index particles

CONTRIBUTION TO SCATTERING BY VARIOUS SIZE CLASSES

MIE SOLUTIONS FOR

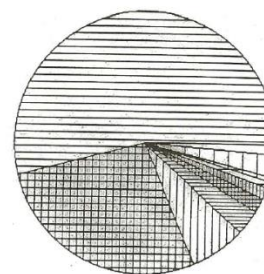
$\lambda = 550 \text{ nm}$

$n = 1.20$ (inorganic particles)

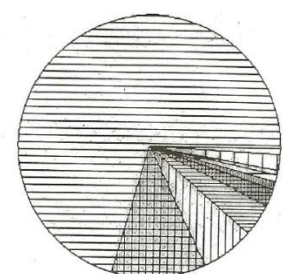
$n' = 0$

$F(D) \sim D^{-4}$

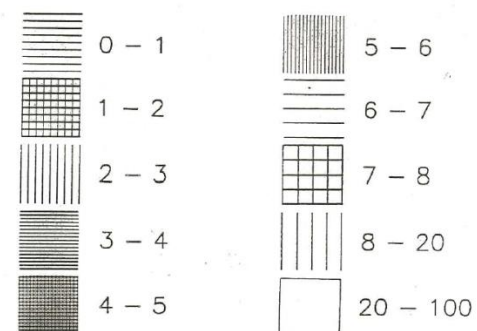
TOTAL SCATTERING



BACKSCATTERING



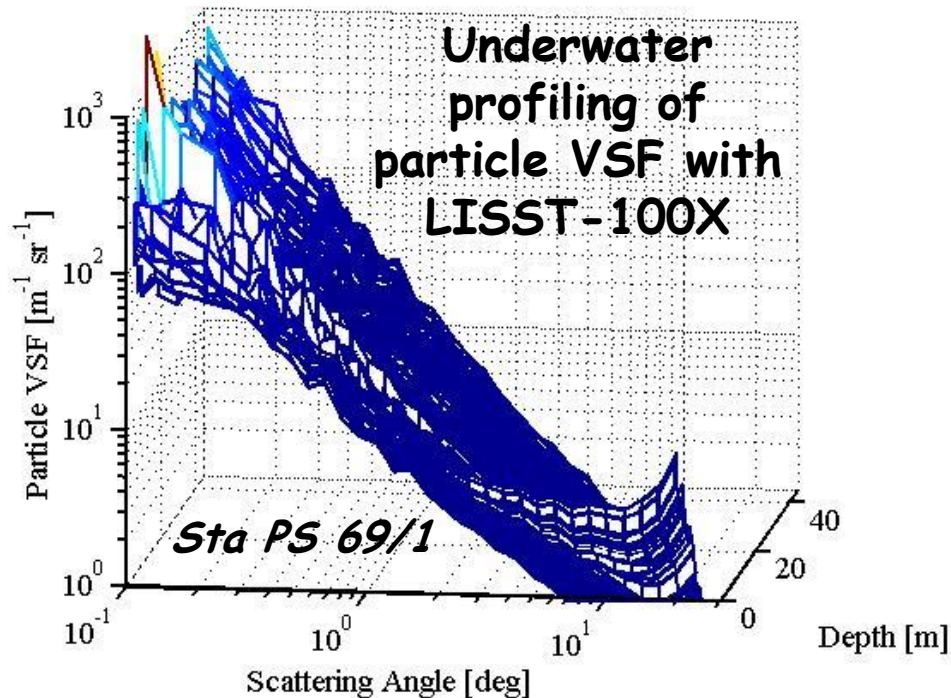
Size classes in micrometers



(Stramski and Kiefer 1991)

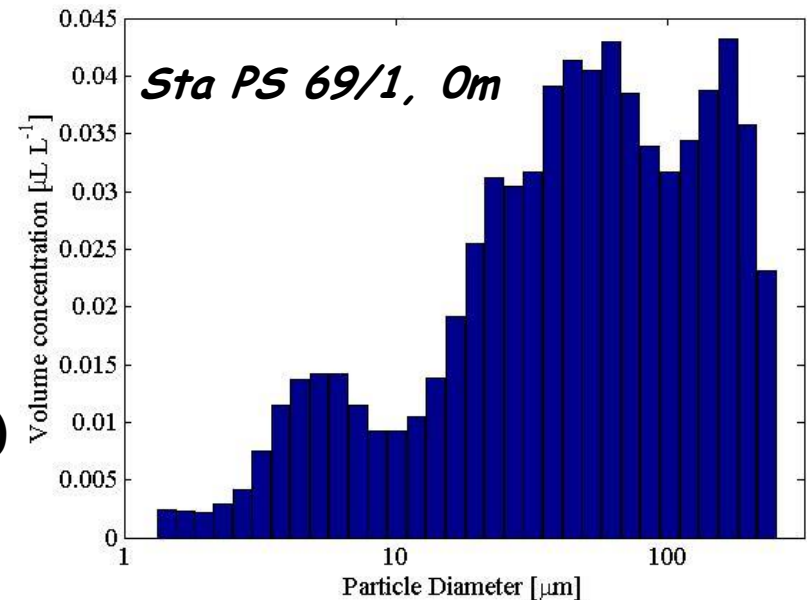
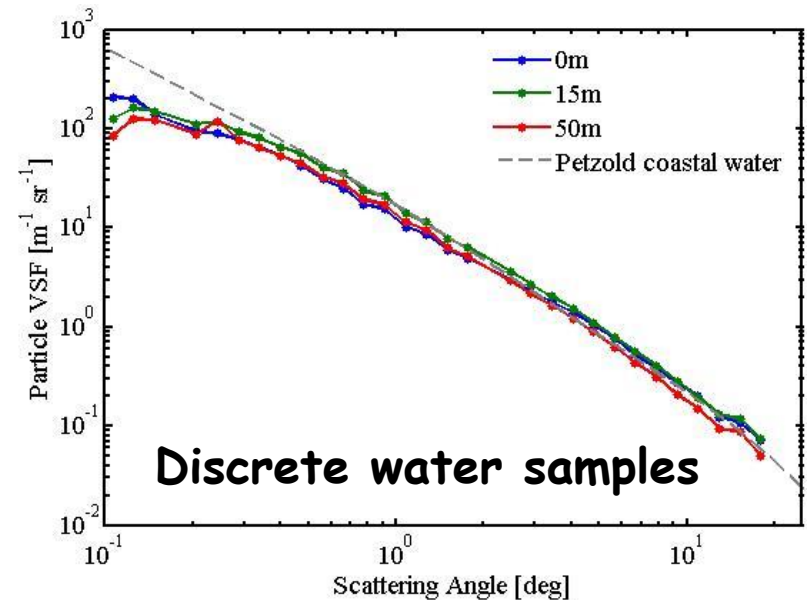
Particle size from light scattering

Laser diffraction particle sizing technique

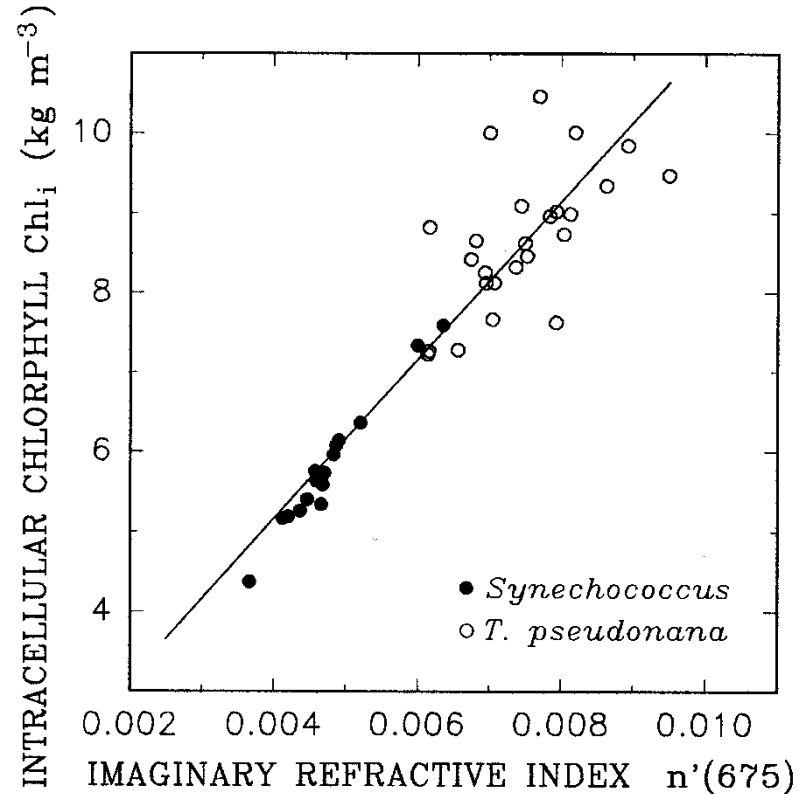
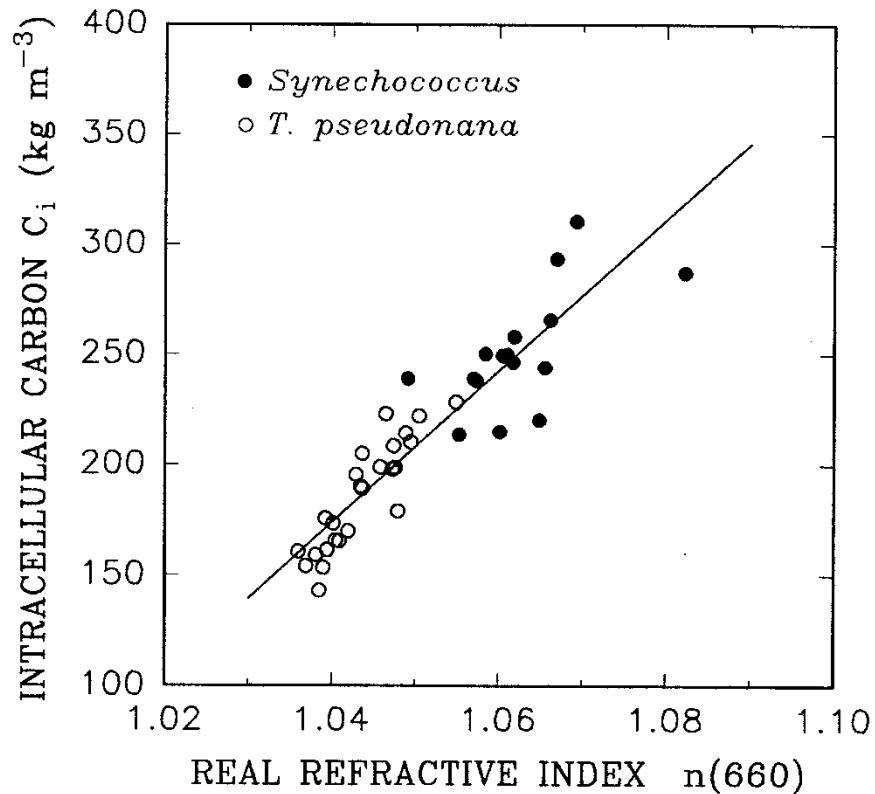


Particle size distribution estimated from Volume Scattering Function (VSF)

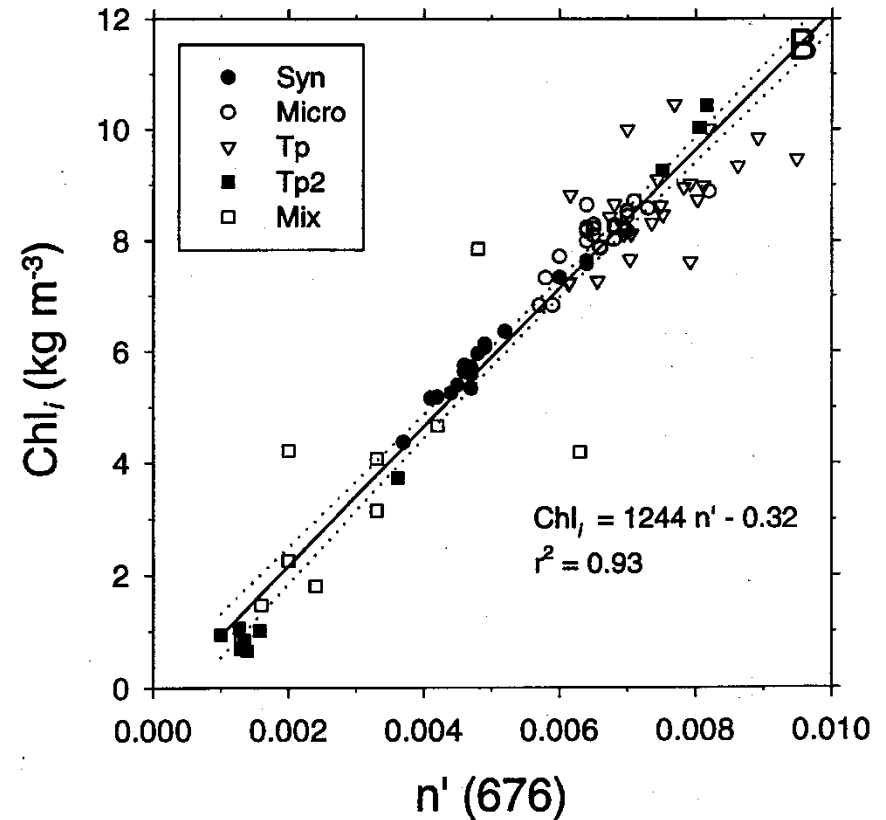
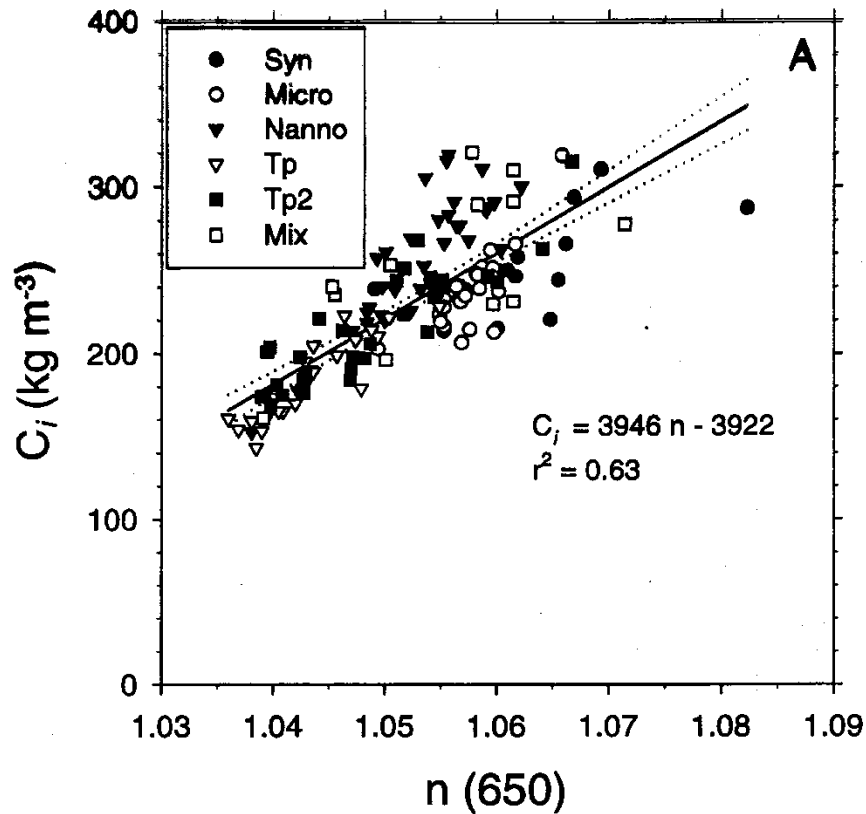
(Unpublished data from the Atlantic Ocean)



Cellular carbon and chlorophyll-a from refractive index

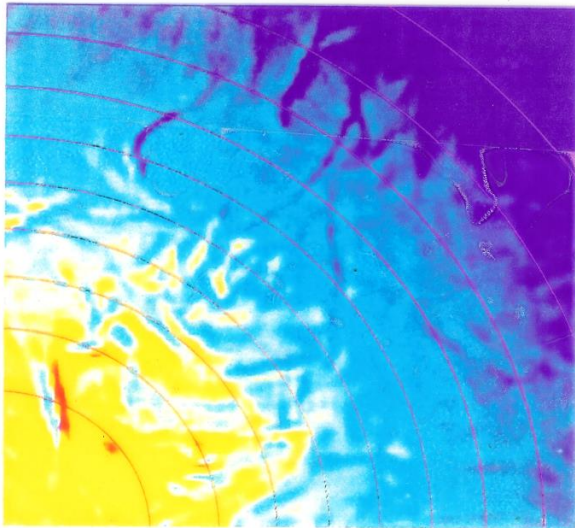
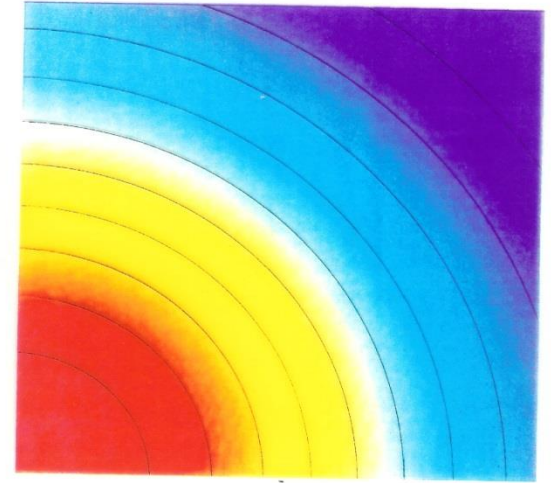


Cellular carbon and chlorophyll from refractive index



Light scattering on turbulence

- The distribution of light intensity in a Gaussian light beam



- The actual distribution of light intensity after propagating the distance of 20 cm within a water volume with turbulence looks like this.

Refractive index n for the extreme values of pressure p , temperature T , salinity S , and wavelength λ , encountered in ocean optics

P (Pa)	T (°C)	S (‰)	λ (nm)	n
1.01×10^5	0	0	400	1.344186
1.01	0	0	700	1.331084
1.01	0	35	400	1.351415
1.01	0	35	700	1.337906
1.01	30	0	400	1.342081
1.01	30	0	700	1.329128
1.01	30	35	400	1.348752
1.01	30	35	700	1.335316
1.08×10^8	0	0	400	1.360076
1.08	0	0	700	1.346604
1.08	0	35	400	1.366885
1.08	0	35	700	1.352956
1.08	30	0	400	1.356281
1.08	30	0	700	1.342958
1.08	30	35	400	1.362842
1.08	30	35	700	1.348986